## **REMARKS**

Pursuant to 37 C.F.R. §1.111, reconsideration of the instant application, as amended herewith, is respectfully requested. Entry of the amendment is requested.

Claims 1-111 are presently pending before the Office. Claims 12, 26, 51, 63, 65, 90, 92, 93, 94 and 99 have been canceled, and claims 102-111 have been added. Applicant has amended claims by the addition of claims. No new matter has been added. Support for the amendments can be found throughout the specification as originally filed. Applicant is not intending in any manner to narrow the scope of the originally filed claims.

The Examiner's Action mailed November 10, 2003 (Paper No. 8) and the references cited therein have been carefully studied by Applicant and the undersigned counsel. The amendments appearing herein and these explanatory remarks are believed to be fully responsive to the Action. Accordingly, this important patent application is believed to be in condition for allowance.

Applicant acknowledges and appreciates the request made by the Examiner to provide information as delineated in paragraph 2 of the Office Action under 37 CFR 1.105. Applicant herein submits his good faith Rule 132 affidavit attached herein, providing to the best of his knowledge, the information desired by the Examiner.

Relying on 35 U.S.C. §112, second paragraph, the Office has rejected the subject matter of claims 1-101 as being indefinite for failing to particularly point out and distinctly claim the subject matter which Applicant regards as the invention. The Examiner alleges that it is unclear

what molecules, dimers and atoms are being claimed. Applicant respectfully traverses the rejection and requests reconsideration.

Applicant submits that ALL kind of molecules, dimers and atoms can indeed form a magnecule without any restriction.

Also, magnecules have been proved to exist at the gaseous, liquid and solid state.

Alternatively, any gas magnecule can be brought to the solid state via cryogenic means during which the magnecular structure IS NOT lost because we decrease the temperature (not so for a magnecule at the solid state that can be lost under sufficient heat).

Therefore, Applicant submits that claims 1-101 do define the legal metes and bounds of the invention. It is not the role of the claims to enable one skilled in the art to reproduce the invention but rather to define, for those skilled in the art the legal metes and bounds of the invention.

It is respectfully submitted that claims 1-101 and new claims 102-121 fully comply with 35 U.S.C. §112, second paragraph. Withdrawal of the rejection is respectfully requested.

Relying on 35 U.S.C. §103(a), the Examiner has rejected the subject matter of claims 1-15, 18-21, 29-45, 52-67, 79-95 and 101 as obvious over Richardson (the '656 patent). Applicant respectfully traverses the rejection and requests reconsideration.

Applicant herein incorporates by reference the attached Affidavit of Applicant Ruggero Maria Santilli submitted under 37 CFR 1.131 and 1.132, wherein applicant submits that the parent application predates the filing of the Richardson patent, and that Richardson admits that an eminent scientist is the inventor of the magnecule and implicitly states that it was discovered

before the filing of his application. Further, Applicant provides an affidavit of Leon Toups of

Toups Technology wherein he verifies that Applicant was in possession of the invention prior to

Mr. Richardson and that Mr. Richardson was in an employee position that allowed him access to

the evidence developed by Applicant.

Accordingly, the Examiner has not established a prima facie case of obviousness.

Applicant notes that pages 15 and 34 of the present application refers to Articles co-

written by Applicant and Donald D. Shillady of Virginia Commonwealth University, Department

of Chemistry, Richmond, Virginia. Although the specification itself discloses the relevant

portion, the complete arrticles are attached herein for the Examiner's perusal and consideration

**CONCLUSION** 

Applicant respectfully submits that claims 1-111 are patentable over the art of record.

A Notice of Allowance is earnestly solicited.

If the Office is not fully persuaded as to the merits of Applicant's position, or if an

Examiner's Amendment would place the pending claims in condition for allowance, a telephone

call to the undersigned at (727) 538-3800 would be appreciated.

Very respectfully.

Dated: 1-26- 200 4

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## HYDROGEN ENERGY

## A new iso-chemical model of the hydrogen molecule

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#### Abstract

Despite outstanding advances throughout this century, we still lack final knowledge on the structure of the hydrogen molecule because of a number of insufficiencies in available models identified in the text. In this paper we use the recently achieved covering of quantum chemistry called hadronic chemistry in its iso-chemical branch, and introduce a new model of the hydrogen molecule characterized by a bond at short distances of the two valence electrons into a singlet quasi-particle state called iso-electronium. We study the iso-chemical model of the hydrogen molecule with a stable iso-electronium describing an oo-shaped orbit around the respective two nuclei, and another model with a weaker realization of the iso-electronium as a partially stable state. We show that the new model provides, apparently for the first time, an exact representation of the binding energy and other characteristics of the hydrogen molecules from axiomatic principles, without ad hoc modifications of theory. In subsequent papers we shall show that the new model permits apparently novel advances in the energy, liquefaction and other technological applications of the hydrogen. © 1999 International Association for Hydrogen Energy. Published by Elsevier Science Ltd. All rights reserved.

## 1. Limitations of quantum chemistry

Unquestionably, quantum chemistry [1-4] constitutes one of the most important scientific achievements of this century whose multiple and diversified applications have produced clear benefits to all of mankind.

Nevertheless, science will never admit 'final theories', and structural generalizations of pre-existing doctrines are only a matter of time.

Doubts on the final character of quantum mechanics, and, therefore, of quantum chemistry, can be traced back to Einstein. Podolsky and Rosen (E-P-R) [5], who introduced their celebrated argument of 'lack of completion' of the theory.

With the advancement of experimental and technological knowledge, more and more limitations of quantum chemistry have been identified, such as

(1) Quantum chemistry does not characterize an attractive force among the neutral atoms of the H- (and other) molecule(s) sufficient to explain their bond. In

fact, the total Coulomb bonding force between atoms is identically null at the semi-classical level. For this reason, the bond is assumed to be due to exchange, van der Waals and other forces originating in nuclear physics whose strength is known to be weak. To state it differently, quantum chemistry still lacks in a molecular bond the equivalent of the strong force in nuclear physics.

- (2) Current models of molecular bonds do not explain why the hydrogen (and water) molecules admit only two H-atoms, and not three or more. In fact, the exchange, van der Waals and other forces were constructed for the specific purpose of admitting an arbitrary number of constituents as necessary to represent nuclei. This main characteristic evidently carries over at the level of molecular bonds, thus preventing a scientific explanation why nature has preferred two hydrogen atoms in the hydrogen and water molecule.
- (3) A number of main characteristics of H- (and other) molecules have not been represented accurately so far by quantum chemistry. This is the case for the binding energy, electric and magnetic dipole and multi-pole moments, liquid state and other aspects which still miss a few percentages in their representation.

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- (4) Quantum chemistry does not allow meaningful thermodynamical calculations. As an example, the 2% currently missing in the representation of molecular binding energies corresponds to about 959 kcal/mole, which is too large an uncertainty for chemical thermodynamics where reaction energies are typically of the order of 20 kcal/mole.
- (5) More accurate numerical representations of molecular data can be achieved via the so-called 'screening of the Coulomb potential' which however constitute a structural departure of the theory from the basic axioms of quantum mechanics and chemistry. As an example, Gaussian screening of the Coulomb law generally requires non-unitary transforms of the original Coulomb settings, thus implying the exiting from the class of equivalence of quantum mechanics and chemistry.
- (6) Current models of molecular bonds imply a behavior of H- (and other) molecules under external electric and magnetic fields contrary to experimental. evidence. As an illustration, the atoms of a molecular bond preserve their individuality according to quantum chemistry. One of the best established disciplines of this century, quantum electrodynamics, then implies that the valence electrons of all atoms of a molecule must assume the same polarization under an external magnetic field. In turn, this implies the capability by water to acquire a paramagnetic character which is contrary to evidence.
- (7) Despite the availability of more powerful computers, accurate configuration interactions converge slowly, thus requiring excessive amounts of computer time for calculations. Such amounts of time increase with accuracy, reaching prohibitive amounts in attempting exact representations.
- (8) The still unexplained 'correlation energy' is at times advocated to treat the missing percentages; orbital theories work well at qualitative and semi-empirical levels, but they remain afflicted by yet unresolved problems, such as the correlation among many electrons as compared to the evidence that the correlation occurs mainly for electron pairs.
- (9) When models achieve 100% representation of the experimental data, this occurs via the introduction of a number of empirical parameters which generally lack physical meaning and motivation; and other problems.

All the above limitations refer to molecular structures which are closed-isolated and reversible (i.e., they verify usual total conservation laws and their time reversal image is causal).

The limitations of quantum chemistry are multiplied when considering irreversible structures, such as chemical reactions involving hydrogen. In fact, we have in this case a structural incompatibility between the basic axioms of quantum chemistry, and the reality represented because said axioms are structurally reversible (as a necessary condition to represent molecules), without any known possibility to modify them in such a way as to reach a credible representation of the irreversibility in chemical reactions from first axiomatic principles.

When passing to more complex biological structures, any claim of final character of quantum mechanics and chemistry implies the exiting of the boundaries of science. In fact, quantum mechanics and chemistry can only represent systems that are closed and isolated from the rest of the universe (conservative), reversible and rigid, as well known. On the contrary, biological systems require the representation of the time rate of variation of characteristics (e.g., their increase at birth, and their decrease at a later age), they are irreversible and flexible. To put it bluntly, under the conditions of the exact validity of quantum mechanics and chemistry everywhere for the microcosm, our body should be perfectly isolated from the rest of the universe, perfectly eternal and perfectly rigid (for studies of these biological aspects one may consult Ref. [15]).

Moreover, biological systems are generally multivalued, in the sense of requiring a structurally novel mathematics expectedly of the so-called hyper-structural type. In any case, the belief of understanding the extremely complex code of a DNA via the single-valued mathematics underlying quantum chemistry is beyond scientific credibility.

In view of these and other occurrences, in this paper we introduce a covering of quantum chemistry which admits the latter as a particular case, yet includes new properties capable of resolving at least some of the above insufficiencies.

We shall then introduce a new model for the structure of the hydrogen molecule which, apparently for the first time, can: explain why the molecule has only two atoms; achieve an exact representation of the binding energy and other characteristics; permit a dramatic reduction of computer time; and reach other advances.

In subsequent papers we plan to indicate that, even though admittedly small, the percentages currently missing in the exact representation of the characteristics of the hydrogen molecule imply rather important technological advances. including possible new structures of the gas itself, new enhancement of the energy content, new means for liquefaction and other applications.

## 2. Rudiments of hadronic mechanics

In this paper we follow the historical E-P-R teaching on the 'lack of completion' of quantum mechanics and, therefore, of quantum chemistry [5-9].

Among a variety of possible 'completions', we study the addition of effects resulting from the deep overlapping of the wavepackets of valence electrons in chemical bonds.

As it is well known, all massive particles (beginning with the valence electrons) have a wavepacket of the order of 1 fm ( $10^{-13}$  cm). We therefore assume quantum chemistry as being exactly valid at distances bigger than 1 fm, while we seek possible, generally small corrections at mutual distances of 1 fm or less due to the deep overlappings of valence electrons.

Deep mutual penetrations of the wavepackets of particles are known to be: non-linear (i.e., dependent on powers of the wavefunctions greater than one), non-local-integral (i.e., dependent on integrals over the volume of overlapping which, as such, cannot be reduced to a finite set of isolated points), and non-potential (i.e., consisting of 'contact' interactions with consequential 'zero range' for which the notion of action-at-a-distance, potential energy has no mathematical or physical sense).

The latter features evidently imply a non-Hamiltonian theory (i.e., a theory which cannot be solely characterized by the Hamiltonian thus requiring additional terms). It then follows that the emerging theory is non-unitary (i.e., its time evolution violates the unitarity conditions UU' = U'U = I when formulated on conventional Hilbert spaces over conventional fields).

In short, we study a 'completion' of quantum mechanics and chemistry via the addition of effects at distances of the order of 1 fm (only) which are assumed to be nonlinear, non-local, non-potential, and non-unitary, here generically referred to as 'non-Hamiltonian effects'. Note that the condition of non-unitarity is necessary to exit the class of equivalence of quantum chemistry.

As it is well known by experts in the field, the main technical difficulty of the above completion is that, when treated via the conventional formalism of quantum chemistry, said short range non-Hamiltonian effects have physical inconsistencies so serious to prevent any consistent application to the real world [11, 16].

To give an idea, we indicate that: non-linear theories violate the superposition principle, thus having no meaningful application to composite systems such as molecules; non-local theories violate causality; non-potential theories violate probability laws; non-Hamiltonian theories do not admit invariant basic units of time, length, energy, etc., thus having no meaningful applications to real measurements; non-unitary theories do not preserve the original hermiticity of operators, thus having no physically acceptable observables; and other inconsistencies (see Refs [11, 16] for details).

Quantitative studies on a non-Hamiltonian completion of quantum mechanics, capable of resolving the above problematic aspects, have been recently permitted by hadronic mechanics [10–21], which is an image of quantum mechanics characterized by the novel iso-, geno- and hyper-mathematics [10] for the representation of reversible, irreversible and multi-valued systems, respectively,

with Hamiltonian as well as non-Hamiltonian effects. It then follows that hadronic mechanics has three corresponding branches called iso-mechanics, geno-mechanics and hyper-mechanics, respectively.

The latter new mathematics are essentially characterized by the lifting of the conventional unit I = +1 of quantum mechanics into invertible generalized units characterized by an  $n \times n$  matrix (or operator)  $\hat{I}$  with an arbitrary functional dependence,  $I = +1 \rightarrow \hat{I} = \hat{I}$  (1.r.r. $\psi$ ,  $\hat{c}\psi$ ,...) = 1/ $\hat{T}$ , which are Hermitean,  $\hat{I} = \hat{I}$ , non-Hermitean,  $\hat{I} \neq \hat{I}$ , and multi-valued-non-Hermitean,  $\hat{I} = (\hat{I}_1, \hat{I}_2, ...) \neq \hat{I}$ , respectively.

The new mathematics then emerge via the reconstruction of all conventional algorithms with respect to said generalized units  $\hat{I}$ , thus including corresponding lifting of numbers and fields, metric and Hilbert spaces, algebras and geometries, etc. For instance, all conventional (associative) products  $A \times B$  of quantum mechanics have to be lifted into the generalized products  $A \times B = A \times \hat{T} \times B$  under which  $\hat{I} = I/\hat{T}$  is indeed the correct left and right new unit,  $\hat{I} \times A = A \times \hat{I} \equiv A$ , called iso, geno- and hyper-units. Similar generalizations hold for all other operations, including differentials and derivatives, conventional and special transforms, etc. [15].

The main physical reason for the lifting of the trivial unit I = +1 into an operator  $\hat{I}$  is that it provides the only known invariant representation of non-Hamiltonian effects in the pairing of valence electrons [16].

To state it differently, in order to prevent possible misrepresentations of reality, contact-non-potential effects should be represented with anything except a (Hermitean) Hamiltonian. All representations of such effects other than that via Hamiltonians have been proved to be non-variant, thus unsuitable for applications. The representation of contact-non-potential effects via generalized units has been selected because it is the sole known approach yielding an invariant theory which, as such, admits predictions suitable for experimental verifications.

As a simple example, the representation of the novel interactions caused by deep wave-overlappings of the valence electrons as in Fig. 1 can be only done in quantum mechanics and chemistry via the addition of potentials in the Hamiltonian. However, this implies granting potential energy to contact effects which have none (it would be like representing the drag force experienced by the space-shuttle during re-entry with a Hamiltonian), thus implying the description of a system that has no connection with physical reality.

A consistent representation of the same non-Hamiltonian interaction of Fig. 1 can be easily achieved by hadronic mechanics via the generalized unit called isounit

$$\hat{I} = \exp\left[C \int d^3 r \psi_1^{\dagger}(r) \psi_1(r)\right]. \tag{2.1}$$

where C is a constant (at short range) and  $\psi_1$ ,  $\psi_4$  are the

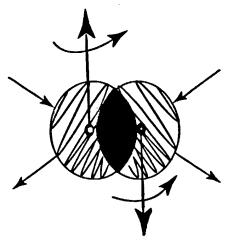


Fig. 1. A schematic view of the fundamental conditions studied in this paper, the deep overlapping of the wavepackets of valence electrons in singlet coupling, as required by Pauli's principle, whose non-linear, non-local and non-potential structure is beyond the capabilities of quantitative treatment via quantum mechanics and chemistry, thus requesting a covering theory.

wavefunctions of the two valence electrons evidently in singlet couplings (from Pauli's principle). Achievement of invariance then requires the step-by-step reconstruction of the entire formalism of quantum mechanics with respect to the new unit (2.1).

Hadronic representation (2.1) of the new interactions of Fig. 1 has a number of advantages over the quantum form, such as: the treatment of non-potential effects without a potential; the achievement of an invariant formulation; the preservation of hermiticity-observability under non-Hamiltonian effects; and others [14, 15].

Whenever the wave-overlapping is no longer appreciable, the exponent of generalized unit (2.1) is null. Then  $\hat{I} \equiv +1$ , and hadronic mechanics recovers quantum mechanics identically at all levels. This illustrates the covering nature of hadronic over quantum mechanics.

A similar situation occurs for other characteristics which are conceptually, mathematically and physically beyond the representation capabilities of a Hamiltonian, but which admit instead a simple and effective representation via generalized units.

An illustration is given by the representation of actual, extended, non-spherical and deformable shapes of bodies which is impossible for quantum mechanics because it would violate one of its pillars (the rotational symmetry), but which can be readily represented by hadronic mechanics. As an example, a deformable spheroidal ellipsoid can be represented via the iso-unit  $f = \text{Diag.}(n_1^2, n_2^2, n_3^2)$ , where the n's are the variable semi-axes, and the reconstruction of the rotational symmetry with respect to that generalized unit (see Refs [9, 15] for details).

Similarly, Bose-Einstein correlations and condensations are known to be beyond the exact character of quantum mechanics because intrinsically extended in space, thus requiring a suitable non-local topology. Hadronic mechanics can readily represent these effects from first axiomatic principles via an  $n \times n$  generalized unit incorporating off-diagonal elements of type (2.1).

We refer the interested reader to Ref. [11] for an outline of numerous applications and experimental verifications of hadronic mechanics in particle physics, nuclear physics, superconductivity, astrophysics and other fields.

A mathematical motivation for the generalization of the unit is that it permits the reconstruction of the linear. local and potential characters on certain generalized spaces (called iso-, geno- and hyper-spaces) over generalized fields (called iso-, geno- and hyper-fields).

The latter features assure the resolution of the problematic aspects indicated earlier for the conventional treatment of non-Hamiltonian effects. The same features also imply that hadronic mechanics coincides with quantum mechanics at the abstract, realization-free level in all its iso-, geno- and hyper-branches, and merely provides broader realizations of conventional quantum axioms.

In particular, hadronic mechanics preserve all conventional laws and principles of quantum mechanics, such as Pauli's exclusion principle, Heisenberg's uncertainties, causality and probability laws, etc.

The understanding of this note requires a knowledge of hadronic mechanics and its underlying new mathematics that we cannot possibly outline here. Readers are therefore referred to Ref. [10] on the new mathematics, Ref. [11] on the latest formulation of hadronic mechanics, and Ref. [16] on the inconsistencies of conventional formulations of non-Hamiltonian effects.

### 3. Rudiments of hadronic chemistry

In this paper we use the covering of quantum chemistry characterized by hadronic mechanics, here called hadronic chemistry. As such, the new discipline too has three main branches called iso-, geno- and hyper-chemistry for the representation of reversible, irreversible and multivalued chemical structures, respectively, with Hamiltonian (long range) and non-Hamiltonian (short range) effects.

Since the hydrogen molecule is stable and reversible, in this paper we shall focus solely on iso-chemistry.

However, the reader should be aware that, as it occurred for conventional chemistry, iso-chemistry too is insufficient to represent chemical reactions, or, more generally, irreversible complex biological structures. When studying these cases in future papers the use of the broader geno-chemistry and hyper-chemistry, respectively, will be necessary for consistency.

Again, by conception and construction, hadronic and quantum chemistry coincide everywhere, except at distances of 1 fm or less in which the former admits novel contributions over the latter under the exact validity of all conventional quantum laws. As we shall see, the novel short range contributions are generally small, yet they permit the apparent resolution of at least some of the insufficiencies outlined in Section 1.

The completion of quantum into hadronic mechanics along the historical E-P-R teaching is studied in detail in Ref. [9]. The same results hold for the completion of quantum into hadronic chemistry. For this reason, the topic is ignored hereon for brevity.

Quantum mechanics and chemistry have only one formulation, the conventional one [1-4]. On the contrary, hadronic theories have two different formulations [10-21], that on generalized spaces over generalized fields and its projection on conventional spaces over conventional fields [10-16]. The reader should be aware that, to avoid excessive complexities for non-initiated readers, in this paper we shall solely consider the projection of hadronic theories on conventional spaces over conventional fields, and leave the mathematically correct formulation to mathematical studies.

Moreover, systems are characterized by quantum mechanics and chemistry via the sole assignment of the Hamiltonian and the tacit assumption of the simplest possible unit I = +1. By comparison, systems are characterized by hadronic mechanics and chemistry via the assignment of two quantities, the Hamiltonian for the representation of all conventional interactions, plus the generalized unit for the representation of the short range non-Hamiltonian effects.

Despite apparent mathematical complexities, isochemistry can be uniquely and unambiguously constructed in its entirety via a non-unitary transform characterizing precisely the iso-unit

$$U \times U^{\dagger} = \hat{I} \neq I, \tag{3.1}$$

which must be applied to the totality of the conventional formalism as a necessary condition to achieve invariance [16]

This procedure yields the iso-unit itself, the isonumbers, the iso-Hilbert space, etc.

$$I \to U \times I \times U^{\dagger} = \hat{I} = 1/\hat{I}, \quad \hat{T} = (U \times U^{\dagger})^{-1},$$

$$c \to U \times c \times U^{\dagger} = c \times (U \times U^{\dagger}) = c \times \hat{I} = \hat{c},$$

$$A \times B \to U \times (A \times B) \times U^{\dagger}$$

$$= (U \times A \times U^{\dagger}) \times (U \times U^{\dagger})^{-1} \times (U \times B \times U^{\dagger}) = \hat{A} \times \hat{B},$$

$$H \times |\psi\rangle \to U \times (H \times |\psi\rangle)$$

$$= (U \times H \times U^{\dagger}) \times (U \times U^{\dagger})^{-1} \times (U \times |\psi\rangle) = \hat{H} \times |\hat{\psi}\rangle.$$

$$\langle \phi| \times |\psi\rangle \to U \times (\langle \phi| \times |\psi\rangle) \times U^{\dagger}$$

$$= (\langle \phi| \times U^{\dagger}) \times (U \times U^{\dagger})^{-1} \times (U \times |\psi\rangle) \times (U \times U^{\dagger})$$

$$= \langle \hat{\phi} | \hat{\times} | \hat{\psi} \rangle \times \hat{I}, \text{ etc.}$$
 (3.2)

Once achieved via the above simple map, iso-chemistry remains invariant under any other possible non-unitary transform, provided that it is evidently expressed in the iso-unitary form on the iso-Hilbert space over iso-fields, under which we have the invariance of the numerical value of the iso-unit, the invariance of the iso-product (where the numerical value of  $\hat{T}$  is not changed), etc.

$$W \times W^{+} = \hat{I} \neq I, \quad W = \hat{W} \times \hat{T}^{1/2},$$

$$W \times W^{+} \equiv \hat{W} \times \hat{W}^{+} = \hat{W}^{*} \times \hat{W}^{'} = \hat{I},$$

$$\hat{I} \rightarrow \hat{I} = \hat{W} \times \hat{I} \times \hat{W}^{+} = \hat{I},$$

$$\hat{A} \times \hat{B} \rightarrow \hat{W} \times (\hat{A} \times \hat{B}) \times \hat{W}^{+} = \hat{A}' \times \hat{T} \times \hat{B}' = \hat{A}' \times \hat{B}'. \text{ etc.}$$
(3.3)

The main problem of completing chemistry into isochemistry is, therefore, the identification of a transform which is:

- (1) non-unitary for r < 1 fm,  $U \times U^{\dagger} r \approx 1$  fm =  $\hat{I} \neq I$ ;
- (2) unitary for r > 1 fm.  $U \times U^{\dagger} r > 1$  fm = I; and
- (3) capable of representing the desired short-range, nonlinear, non-local and non-potential effects due to the overlapping of the wavepackets of the valence electrons, e.g., as in iso-unit (2.1).

All original axiomatic properties of quantum chemistry are preserved everywhere (including at short distances) and only realized in a broader way. This implies the preservation of all quantum laws and principles, such as Pauli's exclusion principle. Heisenberg uncertainty principle, causality and probability laws, etc.

Regrettably, to remain within the limitation on length of this journal, we cannot provide additional details. A comprehensive presentation of hadronic chemistry, including its application to hydrogen, is forthcoming in Ref. [22].

We should finally mention that, by its very structure, iso-chemistry assures much faster convergence of power series. This can be illustrated by the fact that, any given divergent quantum series can always be turned into an isotopically convergent form via the selection of isotopic elements  $\hat{T}$  sufficiently smaller than one [15], as in the example

$$A(k) = A(0) + k[A, H]/1! + \dots \to \infty, \quad k > 1,$$

$$A(k) = A(0) + k[A, H]/1! + \dots = N < \infty, \quad \hat{T} = k^{-n},$$

$$[A, H] = A \times B - B \times A \cdot [A, H] = A \times H + H \times A. \quad (3.4)$$

As we shall see, the above feature permits the reduction of computer time in chemical calculations by a factor of at least 1000, thus rendering feasible calculations that would be otherwise prohibitive.

Needless to say, the studies presented below are deeply linked to numerous preceding studies in quantum chemistry (see, e.g., Refs [23–28]). In fact, we essentially provide a 'completion' of available contributions via novel non-Hamiltonian effects at short distances without exiting from the axiomatic structure of the theory, as inherent in Coulomb screenings and other ad hoc modifications of quantum chemistry. We shall then show the achievement of exact and invariant representations of main data of the hydrogen molecule. Other advances will be presented in future papers.

#### 4. Iso-chemical molecular bonds

We now present, apparently for the first time, the conceptual foundations of our iso-chemical model of molecular bonds for the simplest possible case of the H<sub>2</sub> molecule. We shall then extend the model to the water and to other molecules in subsequent papers.

Since the nuclei of the two H-atoms remain at large mutual distances, the bond of the H<sub>2</sub> molecule is evidently due to the peripheral electrons, as generally acknowledged [1–4].

Our main assumption is that pairs of valence electrons from two different atoms bond themselves at short distances into a singlet quasi-particle state, here called isoelectronium, which describes an oo-shaped orbit around the respective two nuclei, as it is the case of a planet in certain binary stars.

We should stress that the above hypothesis is strictly prohibited by quantum mechanics and chemistry because of the repulsive Coulomb force which prevents any possible bound state of identical electrons at short distances.

However, as we shall see in the next section, the hypothesis is fully plausible for hadronic mechanics and chemistry because the novel non-Hamiltonian interactions due to deep wave-overlappings become so attractive when in singlet couplings at short distance, to overcome repulsive Coulomb forces.

The above occurrence is important to see that the new model of the hydrogen molecule presented in this paper is strictly impossible for quantum mechanics and chemistry, and requires a covering theory.

Iso-chemistry therefore introduces a new attractive force for the representation of the molecular bond among neutral atoms given by the coupling of valence electrons into singlet states. The binding energy is represented by the orbital motion of the iso-electronium around the respective nuclei.

In this paper we show that the emerging new model of the hydrogen molecule can: provide an exact representation of the binding energy from first axiomatic principles: explain the reason why the hydrogen molecule has only two atoms; achieve a much faster convergence of power series with consequential large reduction in computer times; and permit other advances.

The explanation by iso-chemistry of the reasons why the H- (or water) molecule admit only two hydrogen atoms is inherent in the very notion of iso-electronium. In fact, once two valence electrons are bonded into the iso-electronium, there is no possibility for bonding additional atoms.

The exact representation of the binding energy and other characteristics will be presented in the subsequent sections

Two notions of hadronic chemistry are important for further advances:

- (a) the hadronic horizon, which is the ideal sphere of radius 1 fm outside which quantum chemistry is assumed to be exact and within which hadronic chemistry applies; and
- (b) the trigger, which is given by external (conventional) interactions causing identical electrons to move one toward the other and to penetrate the hadronic horizon against their repulsive Coulomb interactions. Once inside said horizon, the attractive hadronic forces overcome the repulsive Coulomb interaction, resulting in a bound state.

The hypothesis of the bonding of electrons at short distances was first introduced by Santilli [29] in 1978 for the structure of the  $\pi^c$  meson as a hadronic bound state of one electron and one positron. Animalu [30] and Animalu and Santilli [31] extended the model to the Cooper pair in superconductivity as a hadronic bound state of two identical electrons.

In the case of the  $\pi^\circ$  model there is no need of a trigger because the constituents have opposite charges, thus naturally attracting each other. On the contrary, the existence of the Cooper pair does indeed require a trigger, which was identified by Animalu [30] and Animalu and Santilli [31] as being constituted by the Cuprate ions. For the case of an isolated hydrogen molecule, we conjecture that the trigger is constituted by the two H-nuclei which do indeed attract the electrons. We essentially argue that the attraction of the electrons by the two nuclei is sufficient to cause the overlapping of the two wavepackets, thus triggering the electrons beyond the hadronic horizon.

We should finally indicate that the hypothesis of the iso-electronium can also be explained via the use of the intrinsic magnetic moments of the electrons which, in singlet couplings, are opposite to each other, thus implying an attraction that can counterbalance the electric repulsion.

However, the approach requires alteration (called mutation) of the electromagnetic fields of the electrons which is directly representable by the Poincaré-Santilli iso-symmetry [12, 13]; namely, an isomorphic reconstruction of the conventional Poincaré symmetry with

respect to the iso-unit. This requires, for quantitative treatment, the lifting, this time, of relativistic quantum mechanics into relativistic hadronic mechanics which is here ignored for brevity [15].

The latter occurrence also explains that the term 'isoelectronium' is motivated by the fact that its constituents are not ordinary electrons (i.e., unitary representations of the Poincaré symmetry), but rather electrons in mutated forms called iso-electrons (i.e., iso-unitary iso-representations of the Poincaré-Santilli iso-symmetry).

### 5. The stable iso-electronium

We begin our quantitative analysis with the non-relativistic quantum mechanical equation of two ordinary electrons in singlet couplings,  $\mathbf{e}_1$  and  $\mathbf{e}_1$ , represented by the wavefunction  $\psi_{11}(r) = \psi(r)$  and the conventional Schrödinger's equation

$$H \times \psi(r) = \left(\frac{1}{m}p \times p + \frac{e^2}{r}\right) \times \psi(r) = E \times \psi(r). \tag{5.1}$$

To transform this state into the iso-electronium representing the bonding of one valence electron with a valence electron of another atom of generic charge ze, we need first to submit eqn (5.1) to a non-unitary transform  $U \times U^{\dagger} = \hat{I} \neq I$  characterizing the short range hadronic effects, and then we must add the trigger, namely; the Coulomb attraction by the nuclei.

By recalling rules (3.2), this procedure yields the iso-Schrödinger equation for the iso-electronium (see [22] for details)

$$U \times H \times \psi(\beta r) + \text{trigger}$$

$$= U \times H \times U^{\dagger} \times (U \times U^{\dagger})^{-1} \times U \times \psi(r) + \text{trigger}$$

$$= H \hat{\times} \hat{\psi}(r) + \text{trigger}$$

$$= \left(\frac{1}{m} \hat{p} \times \hat{T} \hat{p} \times \hat{T} + \frac{e^{2}}{r} \times \hat{T} - \frac{2e^{2}}{r}\right) \times \hat{\psi}(r) = E_{0} \times \hat{\psi}(r),$$

$$\hat{p} \hat{\times} \hat{\psi}(r) = -i \times \hat{T} \times \nabla \hat{\psi}(r),$$
(5.2)

where  $\hat{\psi} = U \times \psi$ ,  $\hat{H} = U \times H \times U'$ ,  $\hat{p} = U \times p \times U'$ , the factor  $\hat{T} = (U \times U')^{-1}$  in the first Coulomb term originates from the non-unitary transform of model (5.1), while the same factor is absent in the second Coulomb term because the latter is long range, thus being conventional.

The angular component of model (5.2) is conventional [1-4] and it is hereon ignored. For the radial component r = |r| we assume the iso-unit [29-31]

$$\hat{I} = e^{N \times \psi \, \hat{\psi}} \approx 1 + N \times \psi / \hat{\psi}, \quad .$$

$$N = \int dr^3 \hat{\psi}^{\dagger}(r)_1 \times \hat{\psi}(r)_1, \quad .$$

$$\hat{T} \approx 1 - N \times \psi / \hat{\psi}. \quad (5.3)$$

Note that the explicit form of  $\psi$  is of Coulomb type. thus behaving like  $C \times \exp(-b \times r)$ , with C approximately constant at distances near the hadronic horizon of radius  $r_c = 1/b$ , while  $\hat{\psi}$  behaves like  $D \times (1 - \exp(-b \times r))/r$ , with D being also approximately constant under the same range [29]. We then have

$$\widehat{T} \approx 1 - V^h/r = 1 - V_0 \frac{e^{-h \times r}}{(1 - e^{-h \times r})/r}$$
 (5.4)

but the Hulten potential behaves at small distances as the Coulomb one:

$$V^b r \approx 1/b \approx \frac{V_0}{b} \times \frac{1}{r}.$$
 (5.5)

As a result, inside the hadronic horizon we can ignore the repulsive Coulomb force altogether and write

$$+\frac{e^2}{r} \times \hat{T} - \frac{z \times e^2}{r} \approx +\frac{e^2}{r} \times (1 - V^h/r) - \frac{z \times e^2}{r}$$

$$= -V \frac{e^{-h \times r}}{1 - e^{-h \times r}}, \quad (5.6)$$

by therefore resulting in the desired overall attractive force among the identical electrons inside the hadronic horizon, as desired.

By assuming in the first approximation  $|\hat{I}| = \rho \approx 1$ , the radial equation of model (5.2) reduces to the model of  $\pi$  meson or of the Cooper pair, although with different values of V and b, which has been studied in great detail in Refs [29–31], including all necessary boundary conditions. The solution is the typical one of the Hulten well:

$$|E_0| = \frac{\rho^2 \times \hbar^2 \times b^2}{4 \times m} \left( \frac{m \times V}{\rho^2 \times \hbar^2 \times b^2} \times \frac{1}{n} - n \right)^2.$$
 (5.7)

To reach a numerical solution, we introduce the parametrization as in Ref. [29],  $k_1 = 1/\lambda \times b$ ,  $k_2 = m \times V/\rho^2 \times \hbar^2 \times b^2$ . We note again that, from the boundary conditions,  $k_2$  must be bigger than but close to 1 [29–31]. We therefore assume in first non-relativistic approximation that  $k_2 = m \times V/\rho^2 \times \hbar^2 \times b^2 = 1$ . By assuming that V is of the order of magnitude of the total energy of the iso-electrons at rest as in the preceding models [29–31], we reach the numerical value of the depth of the hadronic well (Hulten potential):

$$V \approx 2 \times \hbar \times \omega \approx 2 \times 0.5 \,\text{MeV} = 1 \,\text{MeV}.$$
 (5.8)

By recalling that  $\rho \approx 1$ , we reach the following numerical value of the radius of the hadronic horizon (radius of the iso-electronium):

$$r_c = b^{-1} \approx (\hbar^2/m \times V)^{1/2} = (\hbar/m \times \omega_0)^{1/2}$$
  
=  $(1.054 \times 10^{-27} \text{ erg sec})^{1/2}$ 

$$(1.82 \times 10^{-27} \,\text{gr} \times 1.236 \times 10^{20} \,\text{Hz})^{1/2}$$
  
=  $6.8432329 \times 10^{-11} \,\text{cm} = 0.015424288 \,\text{bohrs}$   
=  $0.006843 \,\text{Å}$ . (5.9)

It should be noted that: (1) the above value is only an upper boundary in the center-of-mass frame of the iso-electronium, i.e., it is the largest possible value under the assumptions of this section; (2) the value has been computed under the approximation of identically null relative kinetic energy of the iso-electrons with individual total energy equal to their rest energy; and (3) the value evidently decreases with the addition of the relative kinetic energy of the iso-electrons (because this implies the increase of m in the denominator).

The actual radius of the iso-electronium is also expected to vary with the trigger, that is, with the nuclear charges, as supported by the calculations presented in the next sections. This illustrates again the upper boundary character of value (5.9).

The value  $k_1$  is then given by  $k_1 = V/2 \times k_2 \times b \times c_0 = 0.19$ . Intriguingly, the combined two values  $k_1 = 0.19$  and  $k_2 = 1$  for the iso-electronium are quite close to the corresponding values of the  $\pi^{\circ}$  [29] and of the Cooper pair [30, 31].

It is important to see that, at this non-relativistic approximation, the binding energy of the iso-electronium is not only unique, but also identically null.

The notion of a bound state with only one allowed energy level (called 'hadronic suppression of the atomic spectrum') is foreign to conventional quantum mechanics and chemistry, although it is of great importance for hadronic mechanics and chemistry. In fact, any excitation of the constituents, whether the  $\pi^c$ , the Cooper pair or the iso-electronium, causes their exiting the hadronic horizon, by, therefore re-acquiring the typical atomic spectrum. Each of the considered three hadronic states has, therefore, only one possible energy level.

In fact, it is easy to see that the generally finite Hulten spectrum reduces to only one energy value according to

$$|E_0| = \frac{\rho^2 \times \hbar^2 \times b^2}{4 \times m} \left( \frac{m \times V}{\rho^2 \times \hbar^2 \times b^2} - 1 \right)^2$$

$$= \frac{V}{4 \times k_2} \times (k_2 - 1)^2 = 0. \tag{5.10}$$

The additional notion of a bound state with null binding energy is also foreign to quantum mechanics and chemistry, although it is another fundamental characteristic of hadronic mechanics and chemistry. In fact, the hadronic interactions admit no potential energy and, as such, they cannot admit any appreciable binding energy, as typical for ordinary contact zero-range forces of our macroscopic Newtonian reality.

The null value of the binding energy can be confirmed

from the expression of the meanlife of the iso-electronium which can be written [29]

$$\tau = \hbar/4 \times \pi \times \lambda^2 |\hat{\psi}(0)| \times \alpha \times E_{\epsilon}^{\text{Kin}}$$

$$= 7.16 \times 10^4 \times \frac{k_1}{(k_2 - 1)^3 \times b \times c_0} = \infty. \tag{5.11}$$

The full stability of the iso-electronium,  $t = \infty$ , therefore, requires the exact value  $k_2 \equiv 1$  which, in turn, implies  $E_n \equiv 0$ 

According to the above non-relativistic model, the isoelectronium is a stable bound state (at ordinary conditions). This property is at the foundation of our representation of the stability of the H<sub>2</sub> and other molecules. We should, however, indicate that, under a relativistic treatment [11], the iso-electronium admits a small instability due to the exchange, van der Waals and other forces.

By comparison, the Cooper pair is not permanently stable already at the non-relativistic level because its binding energy is very small, yet finite [30], thus implying a large yet finite meanlife. Also by comparison, the  $\pi^{\circ}$  cannot be stable, and actually has a very small meanlife, evidently because the constituents are a particle—antiparticle pair and, as such, they annihilate each other when bound at short distances. By comparison, no such annihilation may occur in the iso-electronium.

Another important result of this section is that the isoelectronium is sufficiently small in size, as per value (5.9), to be treated as a single quasi-particle. This property will permit rather important simplifications in the isochemical structure of molecules studied in the following sections.

By comparison, the Cooper pair has a size much bigger than that of the iso-electronium. This property is fundamental in preventing the Cooper pair taking the role of the iso-electronium in molecular bonds, i.e., even though possessing the same constituents and similar physical origins, the iso-electronium and the Cooper pair are different, non-interchangeable, hadronic bound states because they originate from different triggers and conditions.

The lack of binding energy of the iso-electronium is perhaps the most important information of this section. In fact, it transfers the representation of the binding energy of molecular bonds to the motion of the iso-electronium in a molecular structure, as studied in the following sections.

A novelty of iso-chemistry over quantum chemistry is that the mutual distance (charge diameter) between the two iso-electrons in the iso-electronium could, as a limit case, also be identically null, that is, the two iso-electrons are superimposed in a singlet state. Rather than being far fetched, this limit case is intriguing because it yields the value — 2e for the charge of the iso-electronium, the null value of the relative kinetic energy, and an identically

null magnetic field. This is a perfectly diamagnetic state which evidently allows a better stability of the iso-chemical bond as compared to a quasi-particle with non-null magnetic moment.

Note that, if conventionally treated (i.e., represented on conventional spaces over conventional fields), the non-unitary image of model (5.1) would yield non-invariant numerical results which, as such, are unacceptable (Section 2 and Ref. [16]). This occurrence mandates the use of the covering iso-chemistry and related iso-mathematics which assures the achievement of invariant results.

Note also that the main physical idea of iso-unit (5.3) is the representation of the overlapping of the wavepackets of the two electrons under the condition of recovering conventional quantum chemistry identically, whenever such overlapping is no longer appreciable. In fact, for sufficiently large relative distances, the volume integral of iso-unit (5.3) is null, the exponential reduces to *I*, the non-unitary transform becomes conventionally unitary, and quantum chemistry is recovered identically.

It is also important to see that, under transform (5.3), model (5.1) is implemented with interactions which are: non-linear, due to the factor  $\psi/\hat{\psi}$  in the exponent; non-local, because of the volume integral in (5.3); and non-potential, because it is not represented by a Hamiltonian.

We finally note that the explicit form of the isotopic element  $\hat{T}$ , eqn (5.3b), emerges in a rather natural (and unique) way as being smaller than one in absolute value,  $|\hat{T}| \ll 1$ . This property alone is sufficient to guarantee that all slowly convergent series of quantum chemistry converge faster for iso-chemistry.

# 6. Iso-chemical model of the hydrogen molecule with stable iso-electronium

We are now sufficiently equipped to present, apparently for the first time, the iso-chemical model of the H<sub>2</sub> molecule. The understanding of the reasons why the molecule has only two H-atoms is inherent in the very concept of iso-electronium (Sections 4 and 5). In this section we shall, therefore, identify the equation of structure of the H-molecule. The exact representation of the binding energy and other characteristics is studied in the subsequent sections.

Our foundation is the conventional quantum model of the H<sub>2</sub> molecule [1-4]. The task is that of subjecting such a model to a transform which is non-unitary only at the short mutual distances  $r_c = b^{-1} = r_{12}$  of the two valence electrons (here assumed to be inside the hadronic horizon), and becomes unitary at bigger distances  $f_r \le 10^{-11}$  cm  $\ne I$ ,  $I_r \gg 10^{-11}$  cm = I. This guarantees that our iso-chemical model coincides with the conventional model except for small contributions at  $r_c = b^{-1}$ .

We assume that the state and related Hilbert space can

be factorized in the familiar form (in which each term is duly symmetrized or anti-symmetrized) as in Refs [1-4].

The non-unitary transform we are looking for shall act only on the  $r_{12}$  variable, while leaving all others unchanged. The simplest possible solution is given by  $U(r_{12}) \times U^{\dagger}(r_{12}) = \hat{I} = \exp\left(\left[\psi(r_{12})/\hat{\psi}(r_{12})\right]\right] dr_{12}\hat{\psi}^{\dagger}(r_{12})_{11} \times \hat{\psi}(r_{12})_{21}$ , where the  $\psi$ 's represent conventional wavefunction and the  $\hat{\psi}$ 's represent iso-wavefunctions.

As a variant to the approach of Section 5 yielding the same end results, we construct the model by transforming short-range terms (iso-chemistry) and adding untransformed long-range ones (chemistry), thus resulting in the radial equation

$$\left(-\frac{\hbar^2}{2\times\mu_1}\hat{T}\times\nabla_1\times\hat{T}\times\nabla_2-\frac{\hbar^2}{2\times\mu_2}\hat{T}\times\nabla_2\times\hat{T}\times\nabla_2+\frac{\mathbf{e}^2}{r_{12}}\right)$$

$$\times \hat{T} - \frac{e^2}{r_{1a}} - \frac{e^2}{r_{2a}} - \frac{e^2}{r_{1b}} - \frac{e^2}{r_{2b}} + \frac{e^2}{R} \times |\hat{\psi}\rangle = E \times |\hat{\psi}\rangle. \quad (6.1)$$

By recalling that the Hulten potential behaves at small distances like the Coulomb one, eqn (6.1) then becomes

$$\left(-\frac{\hbar^{2}}{2 \times \mu_{1}} \nabla_{1}^{2} - \frac{\hbar^{2}}{2 \times \mu_{2}} \nabla_{2}^{2} - V \times \frac{e^{-r_{12} \times h}}{1 - e^{-r_{12} \times h}} - \frac{e^{2}}{r_{1a}} - \frac{e^{2}}{r_{2a}} - \frac{e^{2}}{r_{1b}} - \frac{e^{2}}{r_{2b}} + \frac{e^{2}}{R}\right) \times |\hat{\psi}\rangle = E \times |\hat{\psi}\rangle.$$
(6.2)

The above equation does indeed achieve our objectives. In fact, it exhibits a new explicitly attractive force among the neutral atoms of the molecule which is absent in conventional quantum chemistry. The equation also explains the reasons why the H<sub>2</sub> molecule admits only two H-atoms (Section 5). As we shall see in the remaining sections, eqn (6.2) also permits the exact representation of the binding energy, yields much faster convergence of series with much reduced computer times, and resolves other insufficiencies of conventional models.

Our iso-chemical model of the hydrogen molecule, eqns (6.2), can be subjected to an additional simplification which is impossible for quantum chemistry. In our isotopic model the two iso-electrons are bonded together into a single state we have called iso-electronium. In particular, the charge radius of the latter is sufficiently small to permit that in first approximation, for  $r_{12} \ll r_{1a}$  and  $r_{1b}$ , we have  $r_{1a} \approx r_{2a} = r_a$  as well as, separately,  $r_{1b} \approx r_{2b} = r_b$ . Moreover, the H-nuclei are about 2000 times heavier than the iso-electronium.

Therefore, our isotopic model of the H<sub>2</sub> molecule can be reduced to a restricted three-body problem similar to that possible for the conventional H<sub>2</sub> ion [1–4], but not for the conventional H<sub>2</sub> molecule. It consists of two H-protons at rest and the iso-electronium moving around

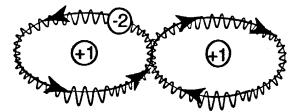


Fig. 2. A schematic view of the proposed iso-chemical model of the hydrogen molecule as well as of other two-body molecules or, more generally, of the bond of one H-atom to a generic other element, e.g., HO, HC, etc., here assumed at absolute K and in the absence of rotations, vibrations, translations and other effects. The fundamental assumption is that the two valence electrons, one per each atom, correlate themselves into a bonded singlet state at a short distance we have called 'iso-electronium'. which is assumed in this case to be stable, with infinite lifetime as in eqn (5.9) and describing an oo-shaped orbit around the respective two nuclei. The iso-electronium is then responsible for the attractive force between the two atoms. The binding energy is instead characterized by the oo-shaped orbit of the isoelectronium around the two nuclei, conceptually represented in this figure via a standing wave. The model then permits a representation of the reason why the H2 and H2O molecules have only two hydrogen atoms, the exact representation of the binding energy and other advances studied in the text.

them in the oo-shaped orbit of Fig. 2, according to the structural equation

$$\left(-\frac{\hbar^{2}}{2\mu_{1}}\nabla_{1}^{2} - \frac{\hbar^{2}}{2\mu_{2}}\nabla_{2}^{2} - V \times \frac{e^{-r_{1};h}}{1 - e^{-r_{1};h}} - \frac{2e^{2}}{r_{o}} - \frac{2e^{2}}{r_{b}} + \frac{e^{2}}{R}\right) \times |\hat{\psi}\rangle = E \times |\hat{\psi}\rangle.$$
(6.3)

Under the latter approximation, the model permits, for the first time, the achievement of an exact solution for the structure of the H-molecule, as it is the case for all restricted three-body problems. This exact solution will be studied elsewhere. In the next sections we shall study the solution of model (6.3) via conventional variational methods.

Note that the above exact solution of the hydrogen molecule is only possible for the case of the fully stable iso-electronium. In fact, for the case of the unstable iso-electronium the model is a full four-body structure which, as such, admits no exact solution.

Note also that model (6.3) is the iso-chemical model of the H<sub>2</sub> molecule inside the hadronic horizon. The matching representation outside the hadronic horizon is presented below. Note also that the above restricted threebody model can be used for the study of the bonding of an H-atom to another generic atom, such as HO, thus permitting, again for the first time, novel exact calculations on the water as HOH: namely, as two intersecting isotopic bonds HO and OH, with possible extension to molecular chains and other molecules.

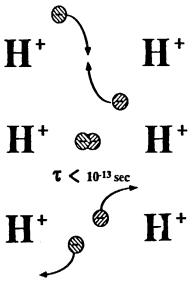


Fig. 3. A schematic view of the iso-chemical model of the hydrogen molecule with unstable iso-electronium due to the weakening of the Hulten potential and consequential relaxation of the infinite lifetime (5.11). In this case the notion of iso-electronium essentially represents a tendency of pairs of valence electrons to correlate in singlet states at short distances. The use of iso-chemistry, rather than conventional chemistry, is necessary because even this weaker form of the iso-electronium, as well as all screenings of the Coulomb potential at large, are non-unitary images of the conventional Coulomb settings as established in Section 5. As such, all these models require a representation on iso-spaces over iso-fields for their invariant formulation. In the text we present the projection of such an invariant formulation on conventional spaces over conventional fields for simplicity.

## 7. Iso-chemical model of the hydrogen molecule with unstable iso-electronium

In this section we study the solution of the restricted iso-chemical model of the hydrogen molecule, eqn (6.3), via conventional variational methods [1–4]. For this purpose we note that the solution of the full model with the Hulten potential  $\exp(-rb)/[1-\exp(-rb)]$ , where  $r_r = b^{-1}$  is the horizon, implies rather considerable technical difficulties. Therefore, we shall study model (6.3) under an approximation of the Hulten potential given by one Gaussian of the type  $[1-A\exp(-br^2)]/r$  with A a constant identified below.

Recall from Section 5 that the stable character of the iso-electronium, eqn (5.11), is crucially dependent on the use of the attractive Hulten potential which 'absorbs' repulsive Coulomb forces at short distances resulting in a strong attraction. Therefore, the weakening of the Hulten potential into the above Gaussian form has the direct consequence of turning the iso-electronium into an unstable state.

In this and in the following sections, we shall, therefore,

study a new iso-chemical model of the hydrogen molecule which is somewhat intermediary between the conventional chemical model and the iso-chemical model with a fully stable iso-electronium.

It should be indicated that the assumption of an unstable iso-electronium implies the capability for more hydrogen atoms to bond to the H-molecules, as well as other features (such as the capability for the hydrogen and water molecules to acquire a paramagnetic character under external magnetic fields) for values depending on the lifetime of the iso-electronium. These features will be studied in detail in subsequent papers.

1.00

The main objective of this section is to show the achievement of the exact representation of molecular characteristics even for the case of one Gaussian approximation of the Hulten potential. Since a sufficient number of Gaussians can reproduce any potential, the achievement of the exact representation with one Gaussian assures its preservation for additional Gaussians, thus also for the Hulten potential.

The question whether the iso-electronium is stable or unstable evidently depends on the amount of instability and its confrontation with experimental data, e.g., on magnetic dipole moments. As such, the issue will be addressed theoretically and experimentally in a future paper.

We begin with the approximation of the Hulten potential with the Coulomb one, and then add a Gaussian 'screening'. The reader should be aware that the latter brings us squarely within the applicability of iso-chemistry because the map from the Coulomb potential to Gaussian screened potentials is generally characterized by a non-unitary transform, thus exiting the class of equivalence of quantum mechanics and chemistry. In fact, model (6.3) was constructed precisely via a non-unitary transform of the conventional quantum model.

Under the above assumption, our first step is, therefore, the study of model (6.3) in an exemplified Coulomb form characterized by the following equation, hereon expressed in atomic units (au) (see Ref. [21] for details):

$$H \times \Psi = (-\nabla^2/4 - 2/r_a - 2/r_b + 1/R) \times \Psi,$$
 (7.1)

where the differences from the corresponding equation for the  $H_2^+$  ion [1–4] are the replacement of the reduced mass ( $\mu =$ ) 2 with 4, and the increase of the electric charge from (e = ) 1 to 2.

The standard method for solving the above equation is the following [1-4, 32, 33]. The variational calculation is set up in matrix algebra form in a non-orthogonal basis set which has been normalized to 1. The metric of this non-orthogonal system of equations (S) is used to set up the orthogonal eigenvalue problem and the eigenvalues are sorted to find the lowest value. H is a Hermitean (square) matrix as well as C and S; E is a diagonal matrix with the energy eigenvalues

$$HC = ESC$$
; define  $C = S^{-1/2}C'$ ,  $HS^{-1/2}C' = ES^{-1/2}C'$ ,  $(S^{-1/2}HS^{+1/2}C') = H'C' = E(S^{-1/2}SS^{-1/2})C' = EC'$ , (7.2)

where the last equation is obtained by multiplying the first equation from the left by  $S^{-1/2}$  and using the unitary property that  $S^{-1/2} = S^{+1/2}$  to form an orthogonal eigenvalue problem. Finally we solve C' by diagonalizing H' and obtain  $C = S^{-1/2}C'$ .

The detailed calculations have been done for both the restricted three-body model of the hydrogen molecule, as well as the full four-body versions. They are rather lengthy and cannot be presented here for brevity. We shall, therefore, only outline the main results below and refer to [22] for a comprehensive presentation, including related references.

#### 8. Summary of results

In order to demonstrate the advantage of the isochemical model using a Gaussian-screened-Coulomb attraction between electrons, a standard Boys-Reeves [22] calculation was carried out. This included all single-and double-excitations (CISD) from the ground state Hartree-Fock-Roothaan SCF orbitals for a 99×99 'codetor' [23-28] interaction. Only the 1s orbitals were optimized with a scaling of 1.191 for the least-energy 6G-1s orbitals, but the basis also included 1G-2s, 2G-2p, 1G-3s, 1G-3p, 3G-3d, Td1G-4sp (tetrahedral array of four Gaussian spheres), and 4G-4f orbitals scaled to hydrogenic values as previously optimized.

The additional basis functions provide opportunity to excite electrons to higher orbitals as is the standard technique in configuration interaction (contrary to the main hypothesis of this work which is that there is an attractive 'hadronic' force for electrons inside the  $r_c$  critical radius). The results of the above calculations are summarized in Table 1 below.

The Boys-Reeves C.I. achieved an energy of -1.14241305 hartrees based on an SCF energy of -1.12822497 hartrees. This was followed by one additional iteration of 'natural orbitals' (CINO) in which the first-order density matrix is diagonalized to improve the electron pairing to first-order [29]. The fact that this procedure lowered the energy only slightly to -1.14241312 hartrees ( $-7.0 \times 10^{\circ}$  hartrees) indicates the 99-configuration representation is close to the lower energy bound using this basis set while the iso-chemistry calculation produced the same exact energy with a comparatively much smaller basis set.

Since the Santilli-Animalu-Shillady LOBE (SASLOBE) has only an  $n^7$  routine for the necessary integral transformation instead of the most efficient  $n^5$  algorithm (n is

| Table I                                      |  |
|--|--|
| Summary of results for the hydrogen molecule |  |

| Species<br>basis screening | Н <sub>2</sub> | H <sub>2</sub> <sup>2</sup> | Н <sub>2</sub> |
|----------------------------|----------------|-----------------------------|----------------|
| ls                         | 1.191          | 6.103                       | 1.191          |
| 2s                         | 0.50           | 24.35                       | 0.50           |
| 2p                         | 0.50           | 24.35                       | 2.36           |
| 3s                         | 0.34           | 16.23                       | •              |
| 3p                         | 0.34           | 16.23                       | •              |
| 3d                         | 0.34           | $-16.2^{1}$                 | •              |
| 4sp                        | 0.25           | 12.18                       | •              |
| 4f                         | 0.25           | 12.18                       | •              |
| Variational energy (au)    | •              | -7.61509174                 | *              |
| SCF energy (au)            | -1.12822497    | *                           | -1.13291228    |
| Cl energy (au)             | -1.14231305    | •                           | *              |
| CINO energy (au)           | -1.14241312    | *                           |                |
| SAS energy (au)            | *              | *                           | 1.174444       |
| Exact energy (au) [30]     | -1.174474      | •                           | - 1.174474     |
| Bond length (bohr)         | 1.4011         | 0.2592                      | 1.4011         |
| Electronium radius (bohr)  | *              | •                           | 0.01124995     |

The negative 3d scaling indicates five equivalent three-sphere scaled to 16.20 rather than 'canonical' 3d shapes.

the number of basis functions), the SASLOBE C.I. runs are somewhat slow and required about 20 h on a 300 MFLOPS Silicon Graphics computer.

With more efficient routines this time can be reduced to about three hours. However, the screened-Coulomb attraction method used a smaller basis and achieved lower energies in a few seconds. It is also estimated that careful spacing of fewer quadrature points in the new integral routine can certainly reduce the SASLOBE run times by a factor of 2 at least.

Therefore, it is clear that iso-chemistry calculations are (conservatively) at least 1000 times faster than a C.I. calculation. Another estimate is that since the new integral corrections require a little more time than the usual Coulomb integrals (but do not take any additional storage space), the computer run-times for an iso-chemistry calculation should only be about three times the runtimes for the corresponding Hartree-Fock-Roothaan calculation in any given basis set.

The extension of the iso-chemical model of the  $H_2$  molecule to other molecules is conceptually straightforward. In particular, the notion of iso-electronium essentially restricts all possible bonds to the established ones, as it is the case for the water molecule.

In order to generalize the underlying quantitative treatment to molecules containing H-to-F, the pole-spike was re-optimized to obtain 100% of the correlation energy below the SCF energy in the given basis set since the SCF energy here was not quite at the Hartree-Fock limit (see Table 1 for details).

The energy obtained here results from the calibration

of the pole-spike to the experimental value of HF and is below the Quantum Monte Carlo energy of Luchow and Anderson [33] which requires hours on a much larger computer, as compared to less than 10 min for this work. In fact, the run times for HF were abut 8 cpu min on a 100 MFLOP Silicon Graphics 'O2' workstation.

The principal value of the pole (9.5 d) was calibrated for 100% energy of HF,  $H_2O$  has two tight sigma bonds and two diffuse lone-pairs so a single compromise value is a good test of the method. In HF the  $F^-$  is nearly spherical so an average  $r_c$  value does a better job of describing the 'correlation hole' of transient iso-electronium.

The computed dipole moments are in excellent agreement with the experimental values. The use of the same pole value for H<sub>2</sub>O and HF degrades the H<sub>2</sub> energy slightly. The results of our studies for H-to-F based molecules are summarized in Table 2 below.

A comparison of the above data (particularly those on computer times) with corresponding data obtained via conventional approaches is instructive.

## 9. Concluding remarks

The fundamental notion of the new model of molecular bonds introduced in this paper is the bonding at short distances of pairs of valence electrons from two different atoms into a singlet quasi-particle state we have called iso-electronium, which travels as an individual particle on an oo-shaped orbit around the two respective nuclei.

<sup>&</sup>lt;sup>2</sup>Three-body Hamiltonian (5.1).

Table 2
Iso-electronium results for selected molecules

|                           | H <sub>2</sub>          | H <sub>2</sub> O  | HF                      |
|---------------------------|-------------------------|-------------------|-------------------------|
| SCF-energy (DH)           | -1.132800¹              | -76.051524        | - 100.057186            |
| Hartree-Fock⁴             |                         |                   | $-100.07185^4$          |
| Iso-energy                | $-1.174441^3$           | $-76.398229^3$    | $-100.459500^3$         |
| Horizon R. (A)            | 0.00671                 | 0.00038           | 0.00030                 |
| QMC energy <sup>4,5</sup> | -1.17447                | $-76.430020^{5}$  | -100.442964             |
| Exact non-rel.            | - 1.174474 <sup>6</sup> |                   | - 100.4595 <sup>4</sup> |
| % correlation             | 99.9 <sup>2</sup>       | 91.6 <sup>2</sup> | 103.8                   |
| SCF-dipole (D)            | 0.0                     | 1.996828          | 1.946698                |
| Iso-dipole (D)            | 0.0                     | 1.847437          | 1.841378                |
| Exp. dipole               | 0.0                     | 1.857             | 1.827                   |
| Times (min:s)             | 0:15.49                 | 10:08.31          | 6:28.48                 |

 $(HD^+)$  Dunning-Huzinaga (10S/6P), [6, 2, 1, 1, 1/4, 1, 1] + H<sub>2</sub>P<sub>1</sub> + 3D1.

Horizon radius in Angstroms.

Run times on an O2 Silicon Graphics workstation (100 MFLOPS max.).

The iso-electronium and related methodology are then assumed to characterize a covering of contemporary chemistry we have called iso-chemistry.

The attractive short-range interactions needed to overcome the repulsive Coulomb force in the iso-electronium structure originate from non-linear, non-local and non-Hamiltonian effects in deep wave-overlappings; they are described by the recently achieved covering of quantum mechanics known as hadronic mechanics [11]; and their invariant formulation is permitted by the recently achieved broadening of conventional mathematics called iso-mathematics [10].

Specific experimental studies are needed to confirm the existence of the iso-electronium, by keeping in mind that the state may not be stable outside a molecule in which the nuclear attraction terms bring the electron density to some critical threshold for binding.

Non-relativistic studies yield a radius of the iso-electronium of  $0.69 \times 10^{-10}$  cm. This 'horizon' is particularly important for iso-chemical applications and developments because outside the horizon the electrons repel one another, while inside the horizon there is a 'hadronic attraction'. The value of the hadronic horizon obtained in this paper for  $H_2$  via a Gaussian-lobe basis set (0.00671 A) confirms the value independently obtained via non-relativistic studies. Nevertheless, the value of the hadronic horizon must also be resolved via experiments. Similar considerations apply also for the depth of the

hadronic well of the iso-electronium which has been estimated at about 1 MeV.

The same non-relativistic studies also predict that the iso-electronium is stable within a molecule, although partially stable configurations also yield acceptable results. The question of the stability vs instability of the iso-electronium must, therefore, also be left to experimental resolutions.

The foundations of the iso-electronium can be seen in a paper by Santilli [29] of 1978 on the structure of the  $\pi^z$ -meson which contains the first identification of the attractive character of non-linear, non-local and non-Hamiltonian interactions due to deep wave-overlappings in singlet coupling (and their repulsive character in triplet coupling). The iso-electronium also sees its foundations in subsequent studies by Animalu [30] of 1994 and Animalu and Santilli [31] of 1995 for the Cooper pair in superconductivity, as well as in other examples of electron bondings existing in nature, such as ball lightning.

The iso-electronium also results in having deep connections with a variety of studies in chemistry conducted throughout this century [23–28, 32, 33], and actually provides the physical-chemical foundations with a more adequate mathematical formulation for most of them.

Therefore, the iso-chemical model of molecular bonds results in being consistent with a number of important occurrences in particle physics, superconductivity, chemistry and other fields, such as:

<sup>&</sup>lt;sup>1</sup>LEAO-6G1S+optimized GLO-2S and GLO-2P.

<sup>&</sup>lt;sup>2</sup>Relative to the basis set used here, not quite HF-limit.

<sup>&</sup>lt;sup>3</sup> Iso-energy calibrated to give exact energy for HF. -

<sup>&</sup>lt;sup>4</sup>Hartree-Fock and QMC energies from Luchow and Anderson.

<sup>&</sup>lt;sup>5</sup>QMC energies from Hammond et al. [22].

<sup>&</sup>lt;sup>6</sup>First 7 sig. fig. from Kolis and Wolniewicz [22].

<sup>&</sup>lt;sup>7</sup>Data from Chemical Rubber Handbook, 61st ed., p. E60.

- (1) The iso-electronium introduces a new attractive force among the neutral atoms of a molecular structure which is absent in quantum chemistry and certainly improves our understanding of the strength of molecular bonds and its stability.
- (2) The iso-electronium permits an immediate interpretation of the reasons why the H<sub>2</sub> and H<sub>2</sub>O molecules only admit two H-atoms.
- (3) The iso-electronium permits the achievement of a representation of the missing 2% in the binding energy, thus allowing meaningful thermodynamical calculations.
- (4) The iso-electronium provides an explanation of the long known, yet little understood Pauli exclusion principle, according to which electrons correlate themselves in singlet when on the same orbit without any exchange of energy, thus via interactions essentially outside the representational capabilities of quantum mechanics and chemistry.
- (5) The iso-electronium is consistent with the known existence of superconducting electron-pairs which bond themselves so strongly to tunnel together through a potential barrier.
- (6) The iso-electronium provides a quantitative model for the explanation of 'electron correlation'. Instead of a complicated 'dance of electrons' described by positive energy excitations, the iso-chemistry explanation is that electrons are energetically just outside the horizon of a deep attractive potential well due to their wavefunctions overlapping beyond the critical threshold of the hadronic horizon.
- (7) The iso-electronium is consistent with the 'Coolomb hole' documented by Boyd and Yee as found from subtracting accurate explicitly-correlated wavefunctions from self-consistent-field wavefunctions. In our studies the 'hole' is re-interpreted as a 'hadronic well'.
- (8) The iso-electronium is also in agreement with the 'bipolaron' calculated for anion vacancies in KCl by Fois, Selloni, Parinello and Car and bi-polaron spectra reported by Xia and Bloomfield.
- (9) The iso-electronium permits an increase of the speed in computer calculations at least 1000-fold.

As we hope to illustrate in future works, a promising feature of the proposed iso-chemical model of the hydrogen molecule is not only the capability to permit accurate representations of experimental data in shorter computer times, but also the capability to predict and quantitatively treat new features and reactions.

### References

[1] Boyer DJ. Bonding Theory, New York: McGraw-Hill, 1968.

- [2] Hanna MW. Quantum Mechanical Chemistry. New York: Benjamin, 1965.
- [3] Pople JA, Beveridge DL, Approximate Molecular Orbits. New York: McGraw-Hill, 1970.
- [4] Schaefer HF. The Electronic Structure of Atoms and Molecules. Reading. MA: Addison-Wesley, 1972.
- [5] Einstein A. Podolsky B, Rosen N. Phys Rev 1935;47:777.
- [6] von Neumann J. The Mathematical Foundations of Quantum Mechanics. Princeton, NJ: Princeton University Press, 1955.
- [7] Bell JS. Physics 1965;1:195.
- [9] Bohm D. Quantum Theory. New York: Dover Publications, 1979.
- [9] Santilli RM. Acta Appl Math 1998;50:177
- [10] Santilli RM. Rendiconti Circolo Matematico Palermo. Suppl. 1996;42:7.
- [11] Santilli R.M. Found Phys 1997:27:625.
- [12] Santilli RM. Nuovo Cimento Lett 1983;37:545.
- [13] Santilli RM. J Moscow Phys Soc 1993;3:255.
- [14] Santilli RM. Elements of Hadronic Mechanics. 2nd ed., vols I and II. Ukraine Academy of Sciences. Kiev. 1995.
- [15] Santilli RM. Isotopic, Genotopic and Hyperstructural Methods in Theoretical Biology, Ukraine Academy of Sciences, Kiev, 1996.
- [16] Santilli RM. Origin, problematic aspects and invariant formulation of classical and quantum deformations. Modern Phys Letters 1998;13:327.
- [17] Kadeisvili JV. Mat Methods Applied Sciences 1996:19:1349.
- [18] Tsagas Gr. Sourlas DS. Algebras, Groups and Geometries 1995;12:1 and 67.
- [19] Tsagas Gr, Sourlas DS. Mathematical Foundations of the Lie-Santilli Theory. Ukraine Academy of Sciences. Kiev. 1962
- [20] L\(\theta\)hmus J, Paul E, Sorgsepp L. Non-associative Algebras in Physics. Hadronic Press. 1995.
- [21] Vacaru S. Interactions, Strings and Isotopes on Higherorder Superspaces. Hadronic Press, 1998.
- [22] Santilli RM, Shillady DD, 'Ab Initio' Elements of Iso-schemistry, In: Trell E et al., editors. Proceedings of Beijing Workshop on Fundamental Open Problems in Science, p. 1999, in press.
- [23] Lewis GN. J Am Chem Soc 1916;38:762.
- [24] Langmuir I. J Am Chem Soc 1919;41:868.
- [25] Frost AA. J Chem Phys 1967;46:3707.
- [26] Bates DR, Ledsham K, Stewart AL. Phil Tran Roy Soc (London) A 1954;246:215.
- [27] Wind H. J Chem Phys 1965;42:2371.
- [28] Boys SF, Proc Roy Soc (London) A 1950;200:542.
- [29] Santilli RM. Hadronic J 1978;1:574.
- [30] Animalu AOE. Hadronic J 1994;17:379.
- [31] Animalu AOE, Santilli RM. Intern J Quantum Chemistry 1995;29:175.
- [32] Nguyen TT. Raychowdhury PN, Shillady DD. J Comput Chem 1984:5:640.
- [33] Mosier C. Shillady DD. Math of Computation 1972;26:1022; cf. program LOBE140 described by Shillady DD and Baldwin S. Int J Quantum Chem. Quantum Biology Symposium 1979:6:105.

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## A new isochemical model of the water molecule

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### Abstract

Despite outstanding advances throughout this century; we still lack final knowledge on the structure of the water molecule because of a number of insufficiencies in available models identified in the text. In a preceding paper we submitted a covering of quantum chemistry called hadronic chemistry in its isochemical branch, and introduce a new model of the hydrogen molecule characterized by a bond at short distances of the two valence electrons into a singlet quasi-particle state called isoelectronium. In this paper we introduce, apparently for the first time, the isochemical model of the water molecule which is characterized by two isoelectronia, one per each H-O dimer and show that the model: (1) introduces a new strong force responsible for the molecular bond; (2) explains the reason why the water molecule has only two hydrogen atoms; (3) provides an accurate representation of the binding energy from the first axiomatic principles without ad hoc modifications; (4) permits a correct representation of electric and magnetic moments; and (5) reduces by at least a factor of 1000 computer usages for calculations due to a much faster convergent series. Experimental verifications, applications and novel predictions of the model are studied in subsequent papers. © 1999 International Association for Hydrogen Energy. Published by Elsevier Science Ltd. All rights reserved.

## 1. Introduction

Water is an extremely important compound on Planet Earth in a biological as well as geophysical sense. For this reason, it has been subjected to comprehensive studies conducted since the beginning of quantitative science with outstanding results (see, e.g., Refs. [1,4,14,38,17,21]).

Despite that, a number of fundamental issues on the structure of the water molecule remain still open at the time of writing. Among them we note: the inability to explain why the hydrogen and water molecules only have two H-atoms (because the admitted forces, such as the exchange and van der Waals forces, are of nuclear type thus, being conceived and applicable for

When passing from the structure of one water molecule to more general profiles, the number of open basic issues increases. For instance, it is generally admitted that quantum chemistry has been unable to provide a systematic theory of the liquid state in general, let alone that of the water in particular.

Also, chemical reactions in general are irreversible,

an arbitrary number of constituents); the binding energy still misses 1 to 2% under the strict implementation of the quantum axioms; accurate representations are based on structural changes of the Coulomb law, such as via Gaussian screenings whose axiomatic implications require a specific study; larger percentages are missing in the representation of electric and magnetic moments (which sometimes even have the wrong sign); calculations continue to require large computer times because of poorly convergent series; we still miss an explanation of the electron 'correlation energy'; and other still open basic issues.

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while the axiomatic structure of quantum chemistry is strictly reversible because the theory is strictly Hamiltonian and all known potential forces are reversible. This results in a seemingly irreconcilable incompatibility of the very axiomatic structure of quantum chemistry with chemical reactions in general, and those involving water in particular. In fact, there is no known rigorous way in which the reversible axiomatic structure of quantum chemistry can be turned into the irreversible form needed to represent irreversible events of the chemical reality.

When passing to water as a constituent of biological entities, the limitations of quantum chemistry reach their climax. In fact, biological structures such as a cell are not only irreversible (because they grow, age and die), but have such a complex structure to require multi-valued theories (also known in mathematics as hyperstructures). The expectation that quantum chemistry, with its reversible and single-valued structure, can effectively represent biological structures and their evolution is beyond the boundaries of science.

In view of the above limitations, in the preceding paper Ref. [2,24–29] we have constructed a covering of quantum mechanics under the name of hadronic mechanics. In essence, the two mechanics coincide everywhere, except the region inside a sphere of radius of the order of 1 fm ( $=10^{-13}$  cm) called hadronic horizon in which the broad theory holds. Hadronic mechanics then results to be a form of 'completion' of quantum mechanics much along the lines of the historical Einstein-Podolsky-Rosen argument, although achieved via the addition of contact, nonHamiltonian, nonlinear, nonlocal and nonpotential forces due to deep overlapping of the wavepackets of particles.

On more technical grounds, hadronic mechanics is based on new mathematics, called iso-geno- and hyper-mathematics for the characterization of generalized reversible, irreversible and multivalued systems, respectively.

On pragmatic grounds, hadronic mechanics can be easily constructed via a step-by-step transform  $UU^{\dagger}$  of all aspects of quantum mechanics which is equal to the unit (unitary) everywhere, except inside the hadronic horizon (where it is nonunitary). NonHamiltonian effects due to deep wave overlappings can therefore, be easily added to a conventional model (when appropriate) via nonunitary transforms of the latter.

Following the construction of hadronic mechanics, the authors have constructed a corresponding covering of quantum chemistry under the name of hadronic chemistry [3,30], which also comprises three different branches, isochemistry for the representation of reversible yet generalized structures; genochemistry for the representation of irreversible structures; and hyperchemistry for the representation of irreversible multivalued structures.

Isochemistry was then applied for the construction of a new model of the hydrogen molecule and proved that it does resolve at least some of the insufficiencies of quantum chemistry, such as an explanation that the molecule has only two H-atoms; a representation of the binding energy exact to the seventh digit; computer calculations which converge at least 1000 times faster than those of quantum chemistry and other advances.

In this paper we shall study the isochemical branch of hadronic chemistry; we shall submit, apparently for the first time, the isochemical model of the water molecule; and we shall show that it does indeed permit the resolution of at least some of the insufficiencies indicated above.

A technical understanding of this paper, requires at least some knowledge of Refs. [2,24-29,3,30] whose review is omitted here for brevity.

## 2. Exactly solvable isochemical model of the water molecule with stable isoelectronium

In the preceding paper Ref. [3] we have introduced the main hypothesis of the isochemical molecular model according to which two electrons from two different atoms bond themselves into a singlet quasistable and quasiparticle state called isoelectronium which describes an oo-shaped orbit around the nuclei, as it is the case for planets in certain binary starts.

The main characteristics of the isoelectronium in the first nonrelativistic approximation were calculated and resulted in being: charge -2e, spin 0, magnetic dipole moment 0, mass 1.022 MeV and radius

$$r_{\rm c} = b^{-1} \approx (\hbar^2/mV)^{1/2} = (\hbar/m\omega_0)^{1/2}$$
  
= 6.8432329 × 10<sup>-11</sup> cm = 0.015424288 bohrs  
= 0.006843 Å. (1)

In the above nonrelativistic approximation, the mean life resulted in being infinite (full stability, see Ref. [3], Section 5 in general and Eq. (5.11) in particular), with the understanding that relativistic corrections are expected to render it finite (partial stability). All conventional forces of current use in chemistry (the exchange, van der Waals and other forces) then hold between the isoelectronium and the remaining electrons.

The model was applied to the isochemical model of the hydrogen molecule and implied: (1) the introduction of a new bonding force given by the Hulten force besides those in current use, which is so strong to overcome the repulsive Coulomb force (see Ref. [3], Section 5 in general and Eq. (5.6) in particular), thus being capable of representing the strong molecular

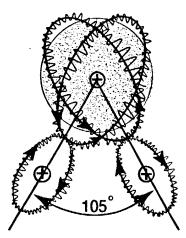


Fig. 1. A schematic view of the proposed isochemical model of the water molecule which is depicted in terms of orbits of the valence electrons (rather than in terms of density distributions) when at absolute zero degrees temperature and in the absence of rotations, vibrations, translations and other motions. The fundamental assumption is that the two valence electrons, one per each pair of atoms, correlate themselves into a bonded singlet state at a short distance we have called isoelectronium, which is assumed to be stable. In this case the only orbit yielding a stable water molecule is that in which the isoelectronium describes an oo-shaped orbit around the respective two nuclei of the H- and O-atoms. The isoelectronium is then responsible for the attractive force between the two atoms. The binding energy is instead characterized by the oo-shaped orbit of the isoelectronium around the two nuclei, conceptually represented in this figure via a standing wave for a particle of spin 0 and charge -2e. In this way the water molecule result in being characterized by two isoelectronia, one per each dimer H-O. The water molecule is then reducible to two intersecting H-O dimers with a common O-atom. Note that, already in the absence of molecular motions, the orbits of the two isoelectronia are perpendicular to the H-O-H plane, thus confirming a characteristic of the water molecule indicated in Ref.[1]. Needless to say, when rotations are added, they imply the rotation of the orbits of the isoelectronia around their individual symmetry axis, resulting in two spherical distributions of the electrons, thus recovering conventional spherical charge distributions. Conventional exchange, van der Waals and other forces then imply the reconstruction of the conventional charge distributions [1]. The model then permits a representation of: (1) the strong value of the molecular bond; (2) the reason why the H<sub>2</sub>O) molecule has only two hydrogen atoms; (3) the exact representation of the binding energy, electric and magnetic moments, and other advances studied in the text. The model of the H-O dimer studied in the text is then extendable to other H-based dimers, such as H-C.

bonds as occurring in reality; (2) the immediate explanation of the reason why the molecule has only two hydrogen atoms, evidently because, once the two elec-

trons of the H<sub>2</sub> molecule are bonded into the isoelectronium, there is no possibility of bonding a third one; (3) a representation of the binding energy of the hydrogen molecule accurate to the seventh digit; (4) a decrease of computer usage for calculation at least 1000 fold; and (5) other advances studied in subsequent papers, such as the impossibility for the molecule to acquire a net magnetic polarity because the two o-branches of the isoelectronium orbit imply opposite rotational motion, with consequently opposite magnetic polarities in agreement with reality.

In this paper we introduce, apparently for the first time, the isochemical model of the water molecule  $H_2O = H - O - H$  considered at °C and in the absence of any rotational, oscillation or other motion. The main hypothesis is that each electron from the two H-atoms couples in singlet with one 2p electron from the O-atom, resulting in two isoelectronia, one per each H-O dimer as in Fig. 1.

According to this model, the bonding force between the two H- and O-atoms is given by the Hulten force between the two valence electrons in the isoelectronia, plus contributions from the conventional exchange, van der Waals and other forces. The binding energy is instead characterized by the two oo-shaped orbits of the isoelectronia around the H-O-H nuclei.

Again, in the first nonrelativistic approximation we shall assume in this section (see next section for a different assumption) that the two isoelectronia of the water molecule are permanently stable and have charges -2e, spin 0, magnetic dipole moment 0, and the same radius as that in the H<sub>2</sub> molecule, Eq. (1). On the contrary, the radii of the two oo-branches of the H-O dimers are expected to be different between themselves, as well as different than the corresponding value in the H<sub>2</sub> molecule.

In this section we shall introduce, apparently for the first time, a hadronic/isoschroedinger equation for the water molecule which is evidently approximate, yet exactly solvable. We shall then show that the model is extendable to all other dimers comprising one hydrogen atom, such as H-C.

For this purpose, we approximate the H-O-H molecule as being composed of two intersecting identical dimers H-O with evidently only one oxygen atom. This requires a first correction due to the lack of independence of said dimers reviewed in Section 3. Moreover, in each H-O dimer we shall assume that the oxygen appears to the isoelectronium as having only one net positive charge +e located in the nucleus. This evidently requires a second correction which essentially represents the screening of the various electrons of the oxygen. Additional corrections are also in order along conventional lines [1].

A study of these corrections has indicated that they can all be represented via one single Gaussian screening of the Coulomb law of the type

$$\frac{+e}{r} \to \frac{+e(1 \pm e^{-\alpha r^2})}{r},\tag{2}$$

where  $\beta$  is a positive parameter to be determined from experimental data, the sign — applies for the screened O-nucleus as seen from an electron (because of the repulsion caused by the electron clouds of the oxygen), while the sign + applies for the screen O-nucleus as seen from the H-nucleus (because of the attraction this time caused by said electron clouds).

The resulting model is structurally equivalent to the isochemical model of the hydrogen molecule of Ref. [3], except for the modifications indicated about, and can be outlined as follows.

By denoting with the sub-indices 1 and a the hydrogen, 2 and b the oxygen, prior to the indicated screening and in the absence of all hadronic effects, the conventional Schroedinger equation of the H-O dimer with the oxygen assumed to have only one elementary charge +e in the nucleus is given by

$$\left(\frac{1}{2\mu_{1}}p_{1}p_{1} + \frac{1}{2\mu_{2}}p_{2}p_{2} - \frac{e^{2}}{r_{1a}} - \frac{e^{2}}{r_{2a}} - \frac{e^{2}}{r_{1b}} - \frac{e^{2}}{r_{2b}} + \frac{e^{2}}{R} + \frac{e^{2}}{r_{12}}\right) + \psi \rangle = E |\psi\rangle.$$
(3)

As it was the case for the  $H_2$ -molecule, our task is that of subjecting the above model to a transform which is nonunitary only at the short mutual distances  $r_c = b^{-1} = \dot{r}_{12}$  of the two valence electrons (here assumed to be inside the hadronic horizon), and becomes unitary at bigger distances  $\hat{l}_r \leq 10^{-13}$  cm  $\neq I$ ,  $\hat{l}_r \gg 10^{-13}$  cm = I. This guarantees that our isochemical model coincides with the conventional model everywhere except for small contributions at small distances.

We assume that the state and related Hilbert space of systems (3) can be factorized in the familiar form (in which each term is duly symmetrized or antisymmetrized)

$$|\psi\rangle = |\psi_{12}\rangle \times |\psi_{1a}\rangle \times |\psi_{1b}\rangle + |\psi_{2a}\rangle + |\psi_{2b}\rangle \times |\psi_{R}\rangle,$$

$$\mathcal{H}_{Tot} = \mathcal{H}_{12} \times \mathcal{H}_{1a} \times \mathcal{H}_{1b} \times \mathcal{H}_{2a} \times \mathcal{H}_{2b} \times \mathcal{H}_{R}. \tag{4}$$

The nonunitary transform we are looking for shall act only on the  $r_{12}$  variable characterizing the isoelectronium, while leaving all other variables unchanged. The simplest possible solution is given by

$$U(r_{12})U^{\dagger}(r_{12}) = \hat{\mathbf{I}} = e^{[\psi(r_{12})/\hat{\psi}(r_{12})]\int dr_{12}\hat{\psi}^{\dagger}(r_{12})_{1\downarrow} \times \hat{\psi}(r_{12})_{2\uparrow}}, \quad (5)$$

where the  $\psi$ 's represent conventional wavefunction and the  $\hat{\psi}$ 's represent isowavefunctions.

We now construct the isochemical model by transforming short-range terms (isochemistry) and adding untransformed long-range ones (chemistry), thus resulting in the radial equation

$$\left(-\frac{\hbar^2}{2\mu_1}\nabla_1^2 - \frac{\hbar^2}{2\mu_2}\nabla_2^2 + \frac{e^2}{r_{12}}\hat{T} - \frac{e^2}{r_{1a}} - \frac{e^2}{r_{2a}} - \frac{e^2}{r_{1b}} - \frac{e^2}{r_{2b}} + \frac{e^2}{R}\right) |\hat{\psi}\rangle = E |\hat{\psi}\rangle.$$
(6)

By using the derivation of Ref. [3] and by recalling that the Hulten potential behaves at small distances like the Coulomb one, Eq. (6) becomes

$$\left(-\frac{\hbar^2}{2\mu_1}\nabla_1^2 - \frac{\hbar^2}{2\mu_2}\nabla_2^2 - V\frac{e^{-r_{12}b}}{1 - e^{-r_{12}b}} - \frac{e^2}{r_{1a}} - \frac{e^2}{r_{2a}} - \frac{e^2}{r_{2a}} - \frac{e^2}{r_{2a}} - \frac{e^2}{r_{2b}} - \frac{e^2}{r_{2b}} + \frac{e^2}{R}\right) |\hat{\psi}\rangle = E |\hat{\psi}\rangle.$$
(7)

The above model can be subjected to an important simplification. In fact, in the first approximation herein considered, the H-O dimer (7) can be reduced to a restricted three body problem similar to that possible for the conventional  $H_2^+$  ion [1], but not for the conventional  $H_2$  molecule, according to the equation

$$\left(-\frac{\hbar^2}{2\mu_1}\nabla_1^2 - \frac{\hbar^2}{2\mu_2}\nabla_2^2 - V\frac{e^{-r_{12}b}}{1 - e^{-r_{12}b}} - \frac{2e^2}{r_a} - \frac{2e^2}{r_b} + \frac{e^2}{R}\right) |\hat{\psi}\rangle = E |\hat{\psi}\rangle.$$
(8)

The indicated corrections due to the screening of the various electrons in the oxygen and other corrections are needed in the 'sensing' of the O-nucleus by the iso-electronium as well as by the H-nucleus, yielding in this way our final model

$$\left(-\frac{\hbar^{2}}{2\mu_{1}}\nabla_{1}^{2} - \frac{\hbar^{2}}{2\mu_{2}}\nabla_{2}^{2} - V\frac{e^{-r_{12}b}}{1 - e^{-r_{12}b}} - \frac{2e^{2}}{r_{a}} - \frac{2e^{2}(1 - e^{-\alpha r_{b}})}{r_{b}} + \frac{e^{2}(1 + e^{-\alpha R})}{R}\right) |\hat{\psi}\rangle = E |\hat{\psi}\rangle$$
(9)

where  $\alpha$  is a positive parameter and E is half of the binding energy of the water molecule.

Under the latter approximation, the model permits, for the first time to our knowledge, the achievement of an exact solution for the structure of the water molecule which however, exists only for the case of the fully stable isoelectronium. In fact, for the unstable

isoelectronium the model becomes a four-body structure which, as such, admits no exact solution.

Besides being exactly solvable, model (9) exhibits a new explicitly attractive force among the neutral atoms of the H-O dimer which is absent in conventional quantum chemistry; the equation also explains the reasons why the water molecule admits only two H-atoms; as we shall see in the remaining sections, the model also permits the exact representation of the binding energy, electric and magnetic moments; the model also yields much faster convergence of a series with much reduced computer times, and resolves other insufficiencies of conventional models.

Finally, the model is evidently extendable with simple adjustment to an exact solution of other dimers involving the hydrogen, such as H-C. In addition, it permits the identification of electric and magnetic polarizations which are not predictable with quantum chemistry.

# 3. Gaussian approximation of the isochemical model of the water molecule with unstable isoelectronium

The solution of the exactly solvable Eq. (9) will be studied elsewhere. In this section we shall study a Gaussian approximation of the isochemical model of the water molecule in which the Hulten potential is essentially approximated to a certain Gaussian form.

It should be indicated from the outset that such an approximation implies an evident weakening of the Hulten attraction among the two isoelectrons of the isoelectronium which, in turn, implies the instability of the isoelectronium itself, thus reaching a model which is somewhat intermediate between the full isochemical model and the conventional quantum mechanical model of the water.

Despite this approximate character, the results of this section are significant because they show the capability by isochemistry to achieve an essentially exact representation of the binding energy, electric and magnetic moments and other characteristics of the water molecule.

But any potential can be exactly reproduced by a sufficient number of Gaussians, including the Hulten potential. Therefore, the exact representations of this section reached for only one Gaussian can be evidently expected to persist for the full isochemical model.

Finally, Gaussian and other screenings of the conventional Coulomb law are now known to be outside the equivalence class of quantum chemistry because they require a nonunitary transform [3]. The Gaussian approximation of this section is, therefore, fully within the basic, nonunitary, axiomatic structure of hadronic chemistry, while similar screenings have questionable

axiomatic foundations when believed to be part of quantum chemistry.

The results of this second study can be outlined as follows. Since HOOH will be slightly more 'allowed' under collisions of HO<sup>-</sup> with neutral H<sub>2</sub>O and the internal repulsion within the anion could favor the release of  $(2e)^{-2}$  to form OH<sup>+</sup>. Collisions of OH<sup>+</sup> with OH<sup>-</sup> will then further enhance the concentration of HOOH and transport of (-2e) will contribute to the current.

The question here is whether under extreme cases of forced conduction a singlet-pair of electrons (isoelectronium, can be 'triggered' (in the nomenclature of Santilli [6] and Animalu and Santilli [31]) within a water molecule to form and release a -2e charged isoelectronium particle which will provide an additional conduction mechanism analogous to Cooper-pairs of electrons in superconducting solids. Since the energy depth of the  $V_0$  parameter in the isoelectronium Hulten potential of the original 1978 derivation by Santilli [6] and Animalu and Santilli [31] is not known, nor how closely the Gaussian representation fits the Hulten form, we can only match the radius of the two potentials and calculate the energy differences caused by the 'sticky-electrons' model in which a transient form of isoelectronium can occur (the Gaussian potential may well not be deep enough to ensure a permanent bound state for isoelectronium).

The 'sticky-electron' model is a parametric model includes the magnetic dipole attraction between singlet-paired electrons as well as the nonlocal merging of the wave-packets of each electron at short distance. The radius of the Gaussian screening is then determined empirically by fitting the calculated energy as nearly as possible to the most accurate energy values available. As used here it should be emphasized that the off-axis positions of the Gaussian-lobe basis sets [7,8,32-36,9,43,37] ensure that angular correlation is included as well as radial dependence and can include the magnetic dipole attraction of opposite electron spins as well as merger of wavepackets. One radial screening parameter used with off-axis basis sets parametrically covers all forms of short range attraction which may include angular dependence. Thus, the present model can give us an approximate energy difference required to release an electron-pair from OH-.

$$OH^- \rightarrow OH^+ - 2e. \tag{10}$$

It will be seen below that the energy difference between OH<sup>-</sup> and OH<sup>+</sup> as calculated, allowing a transient form of isoelectronium, is well within the voltages accessible using capacitive discharge through water. Such a mechanism which would allow (-2e) particles to flow through water would not be superconductivity

since the freely moving molecules and ions are not constrained to lattice positions as in solids so that resistive  $I^2R$  heating will still occur. This is mainly due to the fact that conduction in liquids occurs by mobility of both anions and cations along with size differences, polarizability differences and special mechanisms such as the hydrogen-bonding 'domino' effect for H<sup>+</sup> transport. In solid-state conduction only the electrons move (ignoring in-place phonon oscillations because the atoms do not travel from one electrode to the other; the apparent motion of positively charged 'holes' is also due to the motion of electrons while the atoms merely oscillate about the mean lattice positions), but in solutions there is two-way traffic with positive and negative ions traveling in the opposite directions and with differing velocities; this will certainly lead to resistive heating even up to the vaporization of the water as well as a high probability of ion collisions. It should be noted that in recent work Zhitenev et al. [10] have measured migration of pairedelectrons to quantum dot wells in Gaas and Boyd and Yee [11] have observed 'bipolaron' electron pairs in alkali halide lattice vacancies. Calculations leading to unexpected bipolarons in crystal lattice vacancies have also been observed by using the method of Fois et al. [12]. These findings in solids lend support to the concept of an electron pair as an individual particle, called isoelectronium here.

The calculations given here do not prove the presence of isoelectronium particles in high current aqueous electrical conduction, they only indicate the energy threshold necessary to form (-2e) within the conducting solution by double-ionization of OH<sup>-</sup>. It is not easy to envision an experiment that would be able to analyze components of a given current due to a multiple ion species in terms of the amount of current due to (-2e) particles and none is proposed here. However, there may be a chemical test for such a mechanism. Once OH- is double-ionized to form OH<sup>+</sup>, collisions with (-2e) particles would regenerate OH- ions just as collisions of H+ with OH- will reform H<sub>2</sub>O and no new species will be evident. However, if OH<sup>-</sup> collides with OH<sup>+</sup> a new chemical species (HO-OH) will be formed that may last long enough in the 'liquid plasma' to behave as a strong oxidizing agent. Thus, organic compounds with double bonds (alkenes) which have negligible conductance could be added to water undergoing a high current flow to cause hydroxylation of such compounds [13] (i.e., conversion of alkenes to epoxides which are then readily hydrolyzed in the presence of H+ to diols). Enhanced concentrations of epoxides and diols would be indirect evidence of double ionization of OH-.

OH<sup>+</sup> + OH<sup>-</sup> → HO-OH
$$CH_2 = CHR + HO - OH \rightarrow CH = CHR + H_2O$$
O

(11)

If isoelectronium can be detected indirectly by a chemical method this would in itself be an important inference on the existence of a two-electron, spin-paired particle. More important, 'isochemical reactions' could be driven by high conduction 'liquid plasma' environments where isoelectronium is at an enhanced concentration.

Another case of interest is that of aqueous 'mixtures' of insoluble organic compounds forming a separate 'oil layer' over water in an intense magnetic field of several Tesla. At normal thermal energy of room temperature kT (RT per mole) the main energy form would be a random Brownian motion. However, in the presence of a strong magnetic field HO<sup>+</sup> and HO<sup>-</sup> would be constrained to favor circular motions in the magnetic field by the 'cyclotron effect', but there is no obvious source of HO<sup>+</sup>. Since two ions of opposite sign charges would be favored to collide by both electrical attraction and by opposite path curvature in a magnetic field, there is an enhancement that when created as a normal result of the (H<sup>+</sup>, OH<sup>-</sup>, H<sup>-</sup>, H<sub>2</sub>O<sub>2</sub>, HO<sub>2</sub>, H<sub>2</sub>O) equilibrium system studied by Pourbaix [5], any natural concentration of HOOH would be augmented by collision of H + with HOO-. In addition there is some slight change that H+ would collide with OH- with sufficient excess energy to produce OH+ and H<sup>-</sup>. Thus, the presence of an intense magnetic field

$$H^{+} + HOO^{-} \rightarrow HOOH, \tag{12a}$$

$$H^{+} + OH^{-} \rightarrow H^{-} + OH^{+}$$
 (12b)

$$OH^{+} + OH^{-} \rightarrow HOOH$$
 (12c)

would cause positive and negative ions to collide more easily while traveling in the opposite rotational arcs in such a way as to enhance the concentration of HOOH which could then epoxidate alkenes and upon hydrolysis would lead to diols. A direct measure of this effect would be to determine the enhanced solubility of alkenes in water. The alkenes are only slightly soluble in water ('oil and water do not mix') but alkenes converted to diols will have a measurably greater solubility in water due to the attached -OH groups. Again, if such enhanced solubility of alkenes in water can be caused by intense magnetic fields, this would be indir-

ect evidence of the existence of an electron-pair par-

Note below in the description of the calculations that the key to this work is that it is easy to calculate the energy of OH<sup>-</sup> when one subtracts a small amount from the two-electron repulsion terms in the usual HFR-SCF treatment due to the attraction of singletpaired electrons at close range within 1.0 picometer. In the recent 'Handbook of Computational Quantum Chemistry' by Cook [14,38] (p. 438) it is noted that solutions to the HFR-SCF scheme may not always exist for anions! However, in the method used here convergence of the HFR-SCF process was normal for an SCF process, presumably because the so-called 'self-energy' error of the Hartree-Fock method [15] (each electron repels all electrons including itself) is largely cancelled by the new attractive terms used here. In effect this description of OH is possible because of the easy convergence of the 'correlated-SCF' process.

The model adopted here is to use the usual Hartree-Fock-Roothaan self-consistent-field equations [16] (which also has some formal flaws such as the self-interaction terms [15]) and question the form of the Coulomb interaction of the electrons. Note that reducing the values of the Coulomb integrals will lower the energy by reducing the electron-electron repulsion while reducing the exchange terms will raise the energy, but the (1/2) factor reduces the effect of the exchange terms. Thus, a reduction of the value of the integrals will lower the energy. Note that Goodgame and Goddard [15] have already recommended reducing the atomic self-energy by subtracting 1.39 eV from Hartree-Fock exchange integrals in the cases of Cr<sub>2</sub> and MO<sub>2</sub>.

FC = ESC;

$$F_{i,j} = H_{i,j} + \sum \sum p_{k,l} [(i,j/k,l) - 1/2(i,k/j,l)],$$
(13a)

$$(i, j/k, l) = \iint \chi_i(1)\chi_j(1)/(1/r_{12})/\chi_k(2)\chi_1(2)d\tau_1 d\tau_2,$$
(13b)

$$P_{i,j} = 2\Sigma_n cn, ic_{n,j}$$
(sum  $n$  only over occupied orbitals). (13c)

The 1995 paper on Cooper pairs by Animalu and Santilli [31] invokes the nonlocal hadronic attractive force evident in the  $\pi^0$ -meson as applied to a pair of singlet-paired electrons which form a boson quasi-particle. However, the 'collapsed' positronium rapidly decays since the particle-antiparticle annihilation takes

place in less than a picosecond. In the electron-electron case it is believed that there may be a stable quasi-particle. After using a nonlocal isotopic nonlinear transformation, the hadronic attraction was transformed back to real-space and modeled with a Hulten potential. In this work considerable effort was made to evaluate the matrix elements for the Hulten potential without success. Examination of the original 1978 paper on positronium collapse by Santilli [6] and Animalu and Santilli [31] revealed that the Hulten potential is not necessarily a unique representation of the hadronic force; at least a linear combination of similar potentials could be used to represent the Hulten if the matrix element of such other potentials could be evaluated. The depth of the screened Gaussian approximation is determined here by requiring that the width at half height of the Gaussian is equal to the 'b' value of the Hulten 'horizon', the radius at which the Coulomb repulsion is zero. Thus, the screened-Gaussian potential probably has a depth which is too shallow, although the  $V_0$  depth parameter for the Hulten potential is not known at present.

This work assumes that until the matrix elements of a two-electron interaction for singlet-pairs can be found for the Hulten potential, a Gaussian-screened-Coulomb potential can be used to describe the real-space form of the hadronic attraction and a parameter fitted to experimental energies the screening exponent probably includes other effects such as the magnetic dipole interaction of two electrons with opposite spin-magnetic-moments. This form has the important property that it can be merged with the general case of the four-center Coulomb or exchange integral derived by Shavitt [17] using the famous Gaussian transform technique.

The Gaussian transform two-electron integral for four Gaussian spheres has been used in a number of Gaussian-lobe basis SCF programs written by Mosier and Shillady [18], Shillady and Baldwin [39], Shillady and Talley [19], Shillady and Richardson [40] and others. It is important to note that the formula is completely general in orientation of four Gaussian sphere lobe-orbitals as well as the distance between two electrons. As modified for description of correlation of two electrons, such a general formula can describe angular correlation as well as distance interaction. Thus, matrix elements of a screened-Coulomb interaction were subtracted from the usual (1/r) Coulomb repulsion to model the real-space form of the hadronic attraction of two electrons. This work added the Gaussian screening as  $\exp(-\alpha r^2)/r$  so that the special properties of Gaussians could be used, especially the properties that the product of two Gaussians form another Gaussian (times a rec-entering factor) and that polar coordinates readily separate into factorable x, y and z components. The goal is to evaluate the two-

| Table I        |         |     |          |            |  |
|----------------|---------|-----|----------|------------|--|
| Isoelectronium | results | for | selected | moleculesa |  |

|  | OH <sup>+</sup>       | ОН-                   | H <sub>2</sub> O                                 | HF  |
|--|-----------------------|-----------------------|--|---|
| SCF-energy (DH) Hartree-Fock <sup>c</sup>                        | -74.860377            | -75.396624            | -76.058000                                       | -100.060379<br>-100.07185°                  |
| Iso-energy <sup>b</sup> Horizon RC (A) QMC energy <sup>c,d</sup> | -75.056678<br>0.00038 | -75.554299<br>0.00038 | -76.388340<br>0.00038<br>-76.430020 <sup>d</sup> | -100.448029<br>0.00030<br>-100.44296°       |
| Exact non-rel. Iso-dipole (D) Exp. dipole                        | 5.552581              | 8.638473              | 1.847437<br>1.84 [2]                             | -100.4595 <sup>c</sup><br>1.8413778<br>1.82 |

<sup>&</sup>lt;sup>a</sup> Notes: (HD<sup>+</sup>) Dunning-Huzinaga (10 S/6P), [6,2,1,1,1/4,1,1] + H2S1 + H2P1 + 3D1.

electron four-center matrix elements of the Gaussianscreened-Coulomb potential shown below.

$$Y(r) = (1 - 2 \exp[-(\alpha r^2)]/r.$$
 (14)

Amazingly, the Gaussian-transform variable 's' can be simply shifted by the 'a' value of the screened-Gaussian exponent and carried through the original derivation until the last step when integration over 's' is required. Alpha is usually a very high number, this work used  $0.13441885 \times .10^7$ . At this point the usual Coulombic interaction resorts to a well-known auxiliary function  $F_0$  which has been studied by Mosier and Shillady [18], Shillady and Baldwin [40] and others. Since both  $s^{1/2}$  and  $(s+\alpha)^{1/2}$  occur in the denominator of the screened-Coulomb form, two poles occur in the integral. A change of variable absorbs the pole due to  $(s+a)^{-1/2}$  and shifts the other pole due to  $(s)^{-1/2}$  to the lower limit of the integral. A smooth spike is evident at the lower limit of the numerical integration using a 70 point Simpson's rule integration (two ranges are used with 20 points more closely spaced near the pole and 50 points for the remaining range).

This work was carried out using 64 bit double precision arithmetic which provides 14 significant figures. A simple offset  $(\delta)$  of  $1.0 \times 10^{-15}$  has provided useful results with this simple offset to avoid numerical overflow. While this pole is formally a problem in needing a continuous function to integrate, numerical integration seems to handle this well out to 14 significant figures; particularly since the routines used for the Coulombic integrals are known to be accurate only to 12 significant figures. The area under the pole-spike is estimated as a narrow triangle upon a rectangle  $1.0 \times 10^{-15}$  wide with the height of the triangle set at  $3.43207 \times 10^{8}$  times the height of the point set  $1.0 \times 10^{-15}$  into the range of integration (the first Simpson point). The present code for this screened-

Coulomb integral is presently slower than the corresponding  $F_0e$  [17] function used for the Coulombic integrals due to the 70 point Simpson integration, but the integrand is nearly flat after the spike at s = 0.0 so that the portion of the integrand can be evaluated more rapidly with fewer points. For the results presented here, the simple offset of the lower limit by  $1.0 \times 10^{-15}$  is adequate for this report. Further details on the auxiliary integral can be found in a previous paper on the H<sub>2</sub> molecule [20,41,42]. Work in progress indicates it may be possible to express the new auxiliary integral to an analytical expression involving the Erf(x) function, but until further checks are completed this work used the Simpson integration. Note the integral is a result of a simplification of a 12-fold integration over the volume elements of two electrons and has been reduced to a one-dimensional integration multiplied by appropriate factors.

### 4. Results

The geometry given for H<sub>2</sub>O by Dunning [20,41,42] was used to carry out the usual HFR-SCF calculation after an additional 3 d orbital mimic [19,40] was optimized for the O-atom and (2 S,2p) orbitals were added for the H-atoms. The exponent for the O3 d orbitals was optimized to three significant figures and the (O3 d,H2 s,H2p) exponents were (2.498, 0.500, 1.000). These polarization orbitals were added to the Dunning-Huzinaga (10s6p) [20,41,42] basis with the H1 s orbitals scales to 1.2 which produced a lower energy than that of a 6-31G\*\* basis using the GAMESS program. The bond length of OH<sup>+</sup> was optimized using GAMESS at the 6-31G\*\* basis level and fund to be 1.0062 Å. The same bond length was used for OH<sup>-</sup> since the anion calculation using the

b Iso-energy calibrated to give maximum correlation for HF.

<sup>&</sup>lt;sup>c</sup> Hartree-Fock and QMC energies from Luchow and Anderson [22].

<sup>&</sup>lt;sup>d</sup> QMC energies from Hammond et al. [21].

usual HFR-SCF process was not feasible and in any case the bond length is only slightly longer than that in water. The horizon cutoff value of 0.00038 Å optimized for  $H_2O$  was also used for  $OH^+$  and  $OH^-$ . The spike in the numerical integral routine was optimized by fitting the  $r_c$  cutoff value so as to obtain as near as possible the non-relativistic energy of the HF molecule as determined from quantum Monte Carlo calculations [21]. The dipole moments for the ions are not very useful since ion dipoles are origin dependent, but they were calculated using the center-of-mass as the origin.

As we see in Table 1, the difference in energy between OH<sup>-</sup> and OH<sup>+</sup> is 0.497621 hartrees (13.54 electron volts) according to the correlated-SCF calculations. It is clear from the standard SCF energy value for H<sub>2</sub>O that this basis is very good, but not quite at the Hartree-Fock limit of energy. In addition, the fitting of the numerical integration spike so as to nearly reproduce the total energy of HF is not exact. These two artifacts introduce an energy uncertainty of about 0.0115 hartrees, but this is less uncertain than that of the quantum Monte Carlo energy of Luchow and Anderson [22]. Note that the iso-dipoles for H<sub>2</sub>O and HF are very close to the experimental values which indicate that the calculated wavefunctions are of high quality as well as the energy values.

Since the ionization energy of a neutral H-atom is 13.60 eV and the energy difference of 13.54 eV would convert OH- to OH+, a threshold of about 13.7 eV should maintain H<sup>+</sup> in a solution as well as transfer (-2e) through an aqueous solution to or from the OH-/OH+ system. These calculations indicate that there may be an enhancement of current flow above a potential above 13.7 V across an aqueous cell and that the enhanced concentration of HOOH may be measurable above a potential of 13.7 V. It is worth repeating that this estimate is possible largely due to the easy convergence of the correlated-SCF process for a negative ion species; a process which is formally not defined under the usual Hartree-Fock-Roothaan process [14,38] and most quantum chemists are familiar with the difficulty in treating negative ions using the standard Hartree-Fock-Roothaan method.

Admitting that the correlated-SCF equations are a parametrized approximation of the Santilli derivation of the Hulten potential [6,31] for a bound electronpair, the method has the advantage of easy incorporation into an existing Hartree-Fock-Roothaan Gaussian basis program merely by subtracting a small 'correlation integral' from the usual two-electron integrals. With some thought one should realize that fitting the single parameter (Gaussian screening exponent,  $\alpha$ ) to experimental energies and/or quantum Monte Carlo results will incorporate another attraction in the form of a magnetic dipole interaction between the spin moment of paired electrons. Including the magnetic

dipole interaction and substituting a Gaussian form for the Hulten exponential potential leaves only a simulation of the bound electron-pair 'isoelectronium' predicted by Santilli. Thus, these results are for a model in which the usual HFT-SCF method is corrected for at least two attractive interactions of electrons causing them to approach each other as if they were 'sticky'; hence the term 'sticky-electron-pair model'.

#### 5. Conclusions

In the preceding paper [3,30] of this series we have presented a covering of quantum chemistry under the name of hadronic chemistry and applied the new discipline to the construction of a new model of molecular structures based on the bonding of a pair of valence electrons from different atoms into a singlet quasi-particle state called isoelectronium. In the preceding paper [3] we then applied the model to the structure of the hydrogen molecule by achieving results such as: a representation of the binding energy and other features of the hydrogen molecule accurate to the seventh digit; an explanation of the reason why the hydrogen molecule has only two hydrogen atoms; a reduction of computer usage at least 1000-fold; and other advances.

In this paper we have applied the isochemical model of molecular bonds to the water and other molecules with similar results. In fact, the isochemical model of the water and other molecules presented in this paper is supported by the following conceptual, theoretical and experimental evidence:

- 1. It introduces a new strong binding force (which is absent in current models) capable to explain the strength and stability of the molecules.
- It explains the reason why the water molecule has only two hydrogen atoms.
- It permits a representation of the binding energy of the water and other molecules which is accurate to several digits.
- It represents electric and dipole moments and other features of the water and other molecules also accurate to several digits.
- It permits a reduction of computer usages in calculations at least 1000-fold; as well as permitting other achievements similar to those obtained for the hydrogen molecule.

Moreover, as it happened for the hydrogen molecule [3,30], the value of the radius of the isoelectronium computed via dynamical equations in Section 3 has been fully confirmed by independent calculations for the water and other molecules conducted via the Gaussian-lobe basis set.

The emission of electron pairs in superconductivity

has been emphasized in the preceding papers. We indicate here preliminary yet direct experimental verifications of the isochemical model of molecular bonds offered by the ongoing experiments on photoproduction of the valence electrons in helium indicating that electrons are emitted in pairs [23]. The systematic repetition of these experiments specifically for water is recommended here. The statistical percentages of electron pairs over the total number of emitted electrons would then establish whether the isoelectronium is fully or only partially stable.

We should also recall that Shillady's computer program of isochemistry, called SASLOBE, has been shown in this paper to be capable of producing an essentially exact representation of experimental data on the water and other molecules 1000 times faster than conventional programs.

We should finally note that the representation of the binding energy, electric and magnetic moments and other characteristics of the water and other molecules exact to several digits confirms a main result of the preceding paper [3,30], namely, the identification of experimental evidence on the insufficiency of quantum mechanics and the validity of the covering hadronic mechanics for the representation of nonlinear, nonlocal and nonpotential—nonunitary effects due to deep overlappings of the 'extended wavepackets' of electrons with a 'point-like charge structure'.

These results evidently provide sufficient credibility to warrant systematic theoretical and experimental studies on the new isochemical model of water and other molecules.

In closing, we would like to indicate, for future study, that the new isochemical model of the water molecule implies new predictions of theoretical and industrial significance. In particular, in a future paper we plan to present theoretical and experimental evidence on an apparent enhancement of the energy content of hydrogen when subjected to certain magnetic and other polarizations.

As additional possibilities we note that, in this work the correlated-SCF method is used to easily obtain an energy for the OH<sup>-</sup> anion in water, while the OH<sup>+</sup> ion is easily treated in either the standard or modified method. The difference in energy between the eight-electron OH<sup>+</sup> system and the 10-electron OH<sup>-</sup> system is found to be 13.54 eV. This represents the energy needed to remove (-2e) from OH<sup>-</sup>. This indicates there may be a threshold for current flow in terms of (-2e) as a quasi-particle in aqueous media at 13.6 eV. This voltage will also maintain H<sup>+</sup> in a solution to some extent. Organic alkenes in a solution should undergo epoxidation followed by solvolysis to diols under the conditions of abundant (-2e).

Another interesting result is that the natural trace amounts of HOOH in water may be increased in water by merely placing the sample in an intense magnetic field. Positive and negative ions will traverse short arc segment paths driven by simple thermal Brownian motion in a way which will lead to an increase in collisions of oppositely charged ions. In particular, OH<sup>-</sup> and OH<sup>+</sup> may undergo collisions more frequently leading to an increase in HOOH.

This additional HOOH should then be available to react with alkenes to form epoxides which will then hydrolyze in water to form diols. Such diols would be much more soluble in water than the original alkenes. This leads to the important possibility that merely exposing water-insoluble alkenes to water in a magnetic field will lead to a chemical reaction of the alkenes to form modified compounds which are more soluble in water. In other words, organic oils containing some double bonds may be made somewhat more soluble in water just by mechanical emulsification of the oils in water in an environment of a high magnetic field.

Thus, mixtures of oils and water could be mechanically agitated in a magnetic field of several Tesla to produce new oils which are chemically similar to the original oils (assuming a large organic structure) but more soluble in water after exposure to the magnetic field. There are numerous important applications of such a process to 'make oils water soluble'.

The industrial applications of the above novel predictions are under development at various corporations and they will be treated in detail in future papers.

### References

- [1] Eisenberg D, Kauzmann W. In: The Structure and Properties of Water. New York: Oxford University Press, 1969. p. 226.
- [2] Santilli RM. In: Elements of Hadronic Mechanics, 2nd ed, vol. I and II. Kiev: Ukraine Academy of Sciences, 1905
- [3] Santilli RM, Shillady DD. Isochemical model of the hydrogen molecule. Int J Hydrogen Energy 1998; (in press).
- [4] Barrow GM. Physical Chemistry, 6th ed. New York: McGraw-Hill, 1996 (Chap. 8).
- [5] Pourbaix M. In: Atlas of Electrochemical Equilibria in Aqueous Solutions. Houston, TX: National Assoc Corrosion Engr, 1974. p. 99.
- [6] Santilli RM. Hadronic J 1978;1:574.
- [7] Boys SF. Proc Roy Soc (London), A 1950;200:542.
- [8] Whitten JL. J Chem Phys 1963;39:349.
- [9] LeRouzo H, Silvi B. Int J Quantum Chem 1978;13:297.
- [10] Zhitenev NB, Ashoori RC, Pfeiffer L, West KW. Phys Rev Letters 1997;79:2308.
- [11] Boyd RJ, Yee MC. J Chem Phys 1982;77:3578.
- [12] Fois ES, Selloni A, Parinello M, Car R. J Phys Chem 1988;92:3268.

- [13] March J. In: Advanced Organic Chemistry. New York: John Wiley and Sons, 1985. p. 733.
- [14] Cook DB. In: Handbook of Computational Quantum Chemistry. Oxford, New York: Oxford Science Publications, 1998. p. 285–95.
- [15] Goodgame MM, Goddard WA. Phys Rev Letters 1985;54:661.
- [16] Schaefer HF. The Electronic Structure of Atoms and Molecules. Reading, MA: Addison-Wesley, 1972.
- [17] Shavitt I. In: Alder B, editor. Methods in Computational Physics. New York: Academic Press, 1963.
- [18] Mosier C, Shillady DD. Math of Computation 1972;26:1022.
- [19] Shillady DD, Talley DB. J Computational Chem 1982;3:130.
- [20] Dunning TH. J Chem Phys 1970;53:2823.
- [21] Hammond BL, Lester Jr WA, Reynolds PJ. Monte Carlo methods. In: Ab Initio Quantum Chemistry, vol.
   1. NJ: World Scientific, 1994. p. 67 (World Scientific Lecture and Course Notes in Chemistry).
- [22] Luchow A, Anderson JB. J Chem Phys 1996;105:7573.
- [23] Burnett Collaboration. hhtp://eve.physics.ox.ac.uk/ INTENSE/.
- [24] Santilli RM. Found Phys 1998;27:625.
- [25] Santilli RM. Rendiconti Circolo Matematico Palermo, Suppl 1996;42:7.
- [26] Santilli RM. Algebras, Groups and Geometries 1993;10:273.
- [27] Santilli RM. Isotopic, Genotopic and Hyperstructural

- Methods in Theoretical Biology. Kiev: Ukraine Academy of Sciences, 1996.
- [28] Sourlas DS, Tsagas GT. Mathematical Foundations of the Lie-Santilli Theory. Kiev: Ukraine Academy of Sciences, 1993.
- [29] Lofihmus J, Paal E, Sorgsepp L. Nonassociative Algebras in Physics. Palm Harbor, FL: Hadronic Press, 1994.
- [30] Santilli RM, Shillady DD. Ab Initio hadronic chemistry. In: Trell E et al, editors. Fundamental Open Problems in Science at the Turn of the Millennium, 1999 (in press).
- [31] Animalu AOE, Santilli RM. Int J Quantum Chem 1995;29:175.
- [32] Sambe H. J Chem Phys 1965;42:1732.
- [33] Preuss H. Z Naturforsch 1956;11a:823.
- [34] Whitten JL, Allen LC. J Chem Phys 1965;43:S170.
- [35] Harrison JF. J Chem Phys 1967:46:1115.
- [36] Frost AA. J Chem Phys 1967;47:3707.
- [37] Nguyen TT, Raychowdhury PN, Shillady DD. J Comput Chem 1984;5:640.
- [38] Cook DB. In: Handbook of Computation Quantum Chemistry. Oxford, New York: Oxford Science Publications, 1998. p. 438-41.
- [39] Shillady DD, Baldwin Sheryl. Int J Quantum Chem, Quantum Biology Symposium 1979;6:105 (cf program LOBE140).
- [40] Shillady DD, Richardson FS. Chem Phys Letts 6:359.
- [41] Dunning TH. J Chem Phys 1971;55:716.
- [42] Dunning TH. J Chem Phys 1971;55:3958.
- [43] LeRouzo H, Silvi B. Int J Quantum Chem 1978;13:311.